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# HILL AND VALLEY DESIGN

THE HILL AND VALLEY DESIGN

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The first part of the paper discusses the importance of understanding the cultural context of the research. It highlights the need for researchers to be sensitive to the values and beliefs of the communities they are studying. This is particularly important in the field of education, where cultural differences can significantly impact learning outcomes. The author argues that a one-size-fits-all approach to education is not only ineffective but also disrespectful to the diverse cultures of our world.

In the second part, the author explores the challenges of conducting research in non-Western contexts. One major challenge is the lack of standardized research methods that are applicable across different cultures. What works in one cultural setting may not work in another. The author provides examples of how researchers have adapted their methods to better fit the needs of their study populations. For instance, some researchers have found that using local languages and involving community members in the research process can lead to more accurate and meaningful results.

The third part of the paper focuses on the ethical considerations of cross-cultural research. It emphasizes the importance of obtaining informed consent from participants, especially in communities where there may be a power imbalance between researchers and the community. The author also discusses the potential for research to be used in ways that could harm the community, and argues that researchers have a responsibility to ensure that their work is for the benefit of the community.

Finally, the author concludes by calling for a more collaborative and respectful approach to cross-cultural research. They suggest that researchers should work with community members as partners rather than as subjects. This approach not only leads to better research outcomes but also helps to build trust and understanding between different cultures.

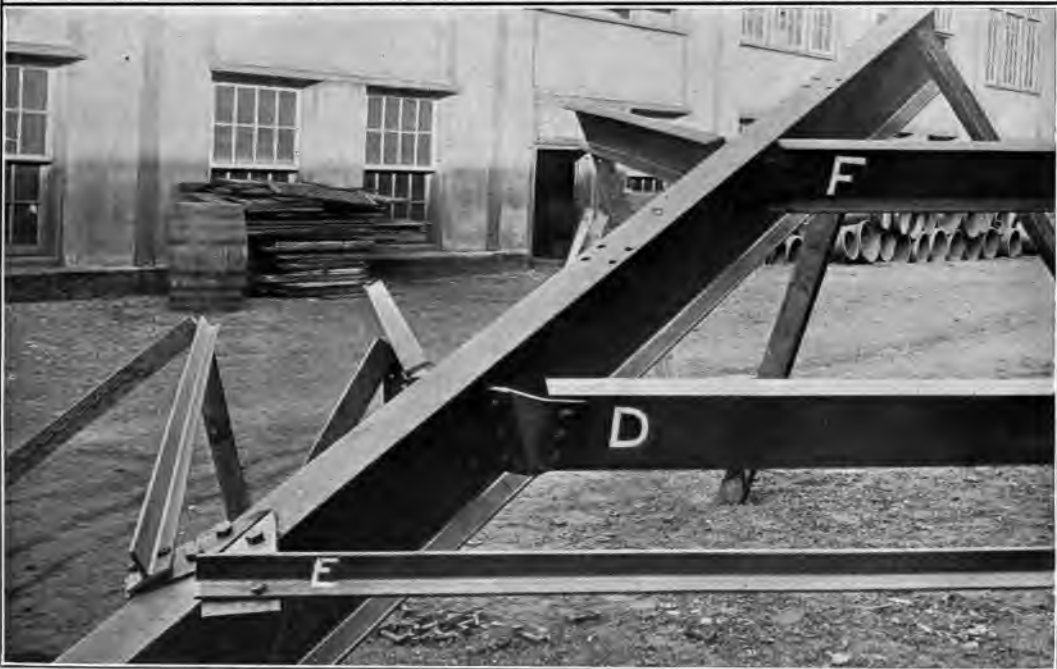
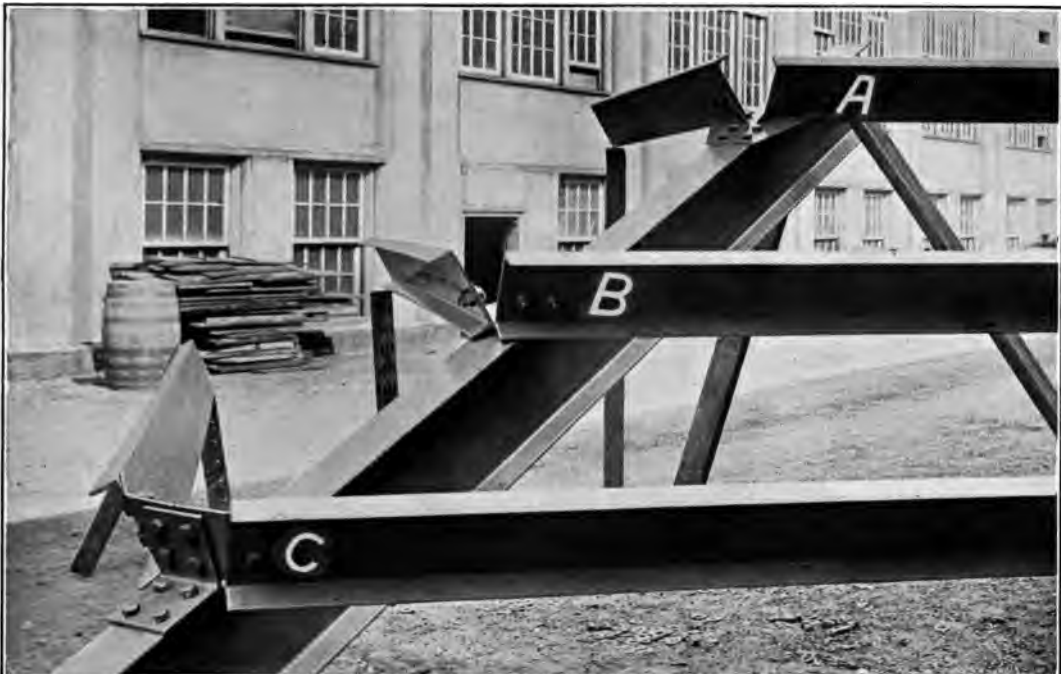








## SIX STYLES OF HIP RAFTER CONNECTIONS



# HIP AND VALLEY DESIGN

DETAILS, FORMULAE AND GRAPHICS

ROOFS

HOPPERS AND PIPE LINES

BY

H. L. McKIBBEN and L. E. GRAY

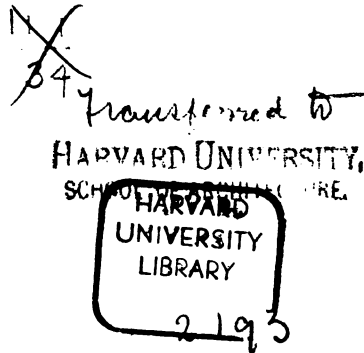
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H. L. McKIBBEN and L. E. GRAY  
Ambridge, Pennsylvania

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## PREFACE.

The difficulty of making working shop drawings for roof connections at Hip and Valley is appreciated by Structural Engineers.

This book has been prepared to cover practical working details for such construction and to present the analytic and graphic processes needful for their development.

From the presentation of the designs here given, Engineers and Architects can determine the style of connection adapted to their demands readily and can specify the same for the structures they have in charge.

To Draftsmen the treatment of the subject will especially appeal, resulting to them in a saving of extra labor and concern.

Students will discover the practical training in descriptive geometry and trigonometry as applied to active engineering to be exceptionally valuable. Class room work in the proof of the formulae is recommended to Engineering Schools.

H. L. McKIBBEN.

L. E. GRAY.

Engineers with American Bridge Co.



## FOREWORD.

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On pages 3, 4 and 5 are shown working details for styles A, B, C, D, E and F, or six methods of connection to Hip Rafters from which to select the one that conforms best to the adjoining framing.

On pages 6, 7 and 8 are found working details for styles A, B, C, D, E and F, or six methods of similar connections to Valley Rafters from which to choose the one most desirable.

A sketch appears with each style of detail showing the position of the purlin in the main roof section, and small sub-formulae showing solutions for the variables  $y_1$  to  $y_{10}$ , with special attention to  $y_1$  and  $y_2$ .

After making selection of style desired, the detailer should solve the angles required as shown in details; i. e.,  $L_8$  and  $L_9$  are needed in style C. No other angles need be found; only those involved in the style chosen.

Solution of these angles can be readily made from general formulae on page 10, if the worker be familiar with Trigonometry and Logarithms; if not, results may be obtained from the simple graphics given on pages 11, 12 and 13, making the problem easy for the detailer who is not familiar with formulae.

If the case in hand be one that is covered by the tabulated solutions on pages 14, 15 and 16, the worker can take from those tables any or all variables which develop in a roof of pitch  $1/5$ ,  $1/4$ ,  $1/3$ ,  $30^\circ$  or  $55^\circ$ , if the angle B in plan is  $30^\circ$ ,  $45^\circ$  or  $50^\circ$ .

These tabulated solutions give the values of the variables for designs in most common use without the necessity of solving any angles whatever; but the formulae on page 10 and graphics on pages 11, 12 and 13 furnish data for solving angles for any roof pitch and all possible positions of rafter.

In styles A, B, C and E the roof line being above the main truss metal line, the worker will need to use formulae on page 9 to locate working point "d."

The authors desire to call especial attention to the following:

1st. The known data are in all cases the main roof pitch or Angle A. The position of Hip or Valley Rafter, Angle B, which is the angle formed by rafter and main truss as seen in *Plan* looking directly perpendicular to lower side of Angle A. No other data than A and B as above described is ever required.

Throughout both details and graphics the letter "d" refers always to the same working point; the marks  $d_1$  and  $d_2$  refer also to this same point, viewed from different positions.

2d. All formulae on page 10 are logarithmic, and in terms of tangent functions.

3d. Use of the graphics on pages 11, 12 and 13 expedite the work and give accurate results.

4th. A short method of graphics for solution of Angles  $L5$ ,  $L6$  and  $L8$  also appears on page 10, which may be used after solving  $L3$  and  $L4$ , if desired.

5th. For those desiring to follow out the proofs given on pages 21 to 29, the four major intersecting planes involved are as follows (see page 10):

#### ROOF PLANE.

Seen in Elevation of Truss as line ab.

Seen in Plan as inclined surface  $a_1$ ,  $b_1$ ,  $r_1$ .

#### PURLIN WEB PLANE.

Seen in Elevation of Truss as line c, d.

Seen in Plan as inclined surface  $d_1$ ,  $c_1$ ,  $e_1$ .

#### RAFTER WEB PLANE.

Seen in Elevation of Rafter as surface  $r_2$ ,  $c_2$ ,  $b_2$ .

Seen in Plan as line  $r_1$ ,  $b_1$ .

#### RAFTER FLANGE PLANE.

Seen in Elevation of Rafter as line  $r_2$ ,  $b_2$ .

Seen in Plan as inclined surface  $r_1$ ,  $b_1$ ,  $e_1$ .

6th. Other formulae which may be used if desired are as follows:

$$\cos L3 = \cos R \cos L1 \sec A.$$

$$\tan L5 = \cos A \tan B \cos L1.$$

$$\tan L5 = \tan L2 \cos L1.$$

$$\tan L7 = \sin A \sin B \cos L4.$$

$$\tan L7 = \cos L2 \tan L10.$$

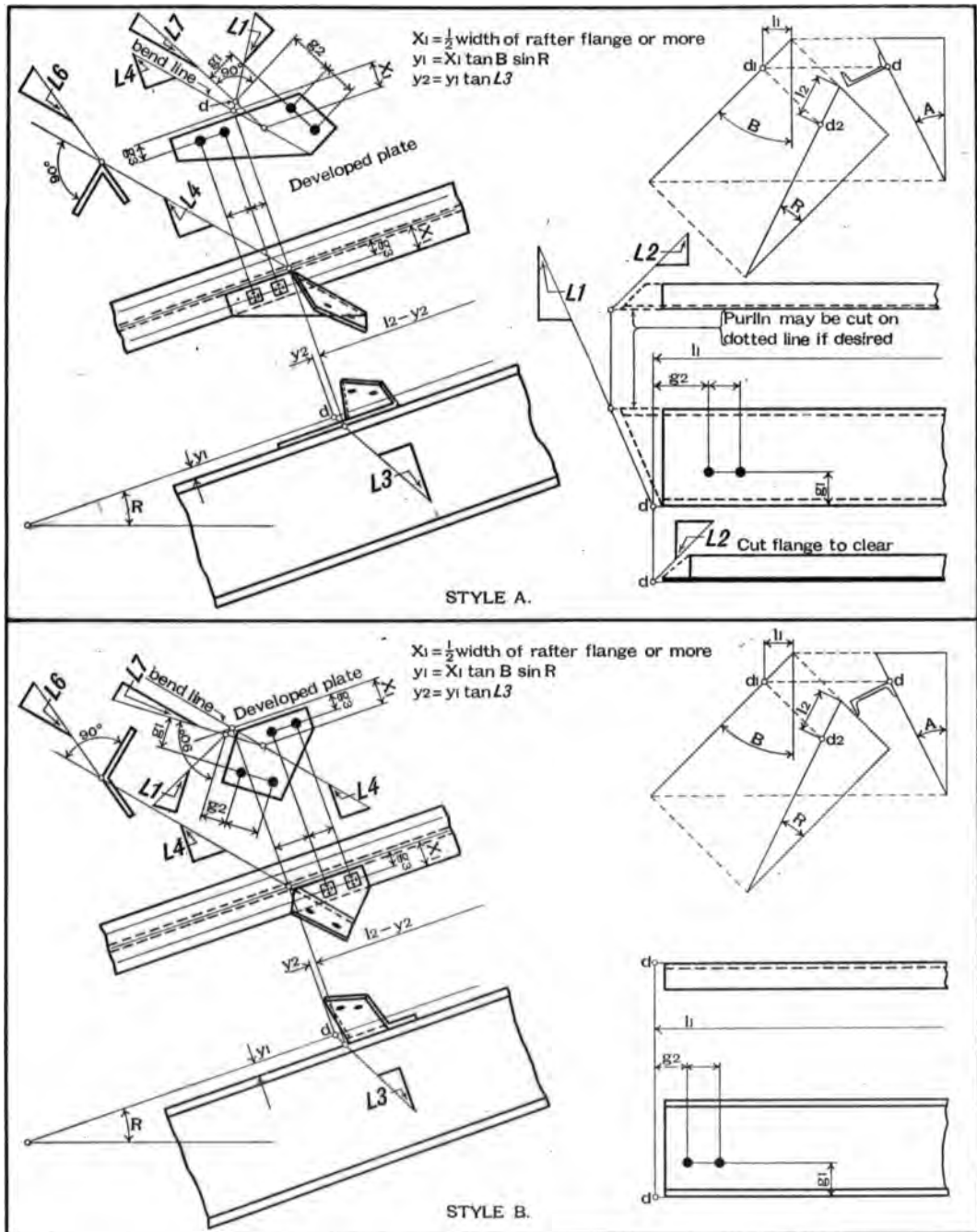
#### HOPPERS, BINS AND CHUTES (FORMS OF VALLEY CONSTRUCTION).

Details for these structures are left to the judgment of the detailer and are usually governed by the main design. The solution of the bend on connecting plate at dihedral intersections is the only difficulty for most draftsmen. Both formulae and graphics are provided on page 17 for ready use.

#### PIPE LINES.

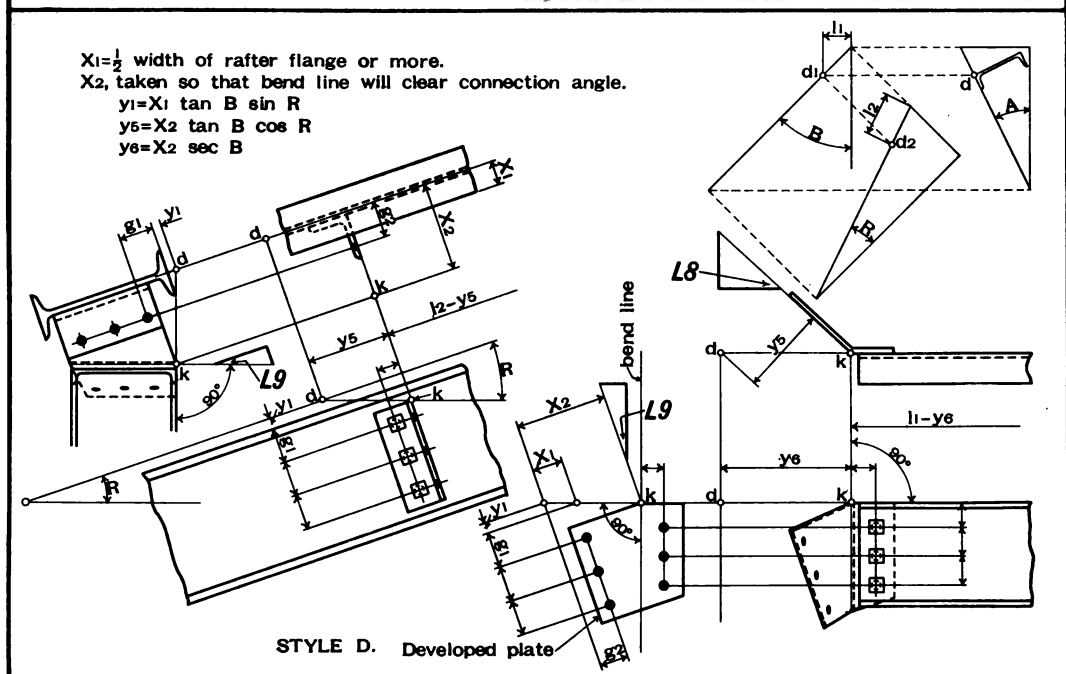
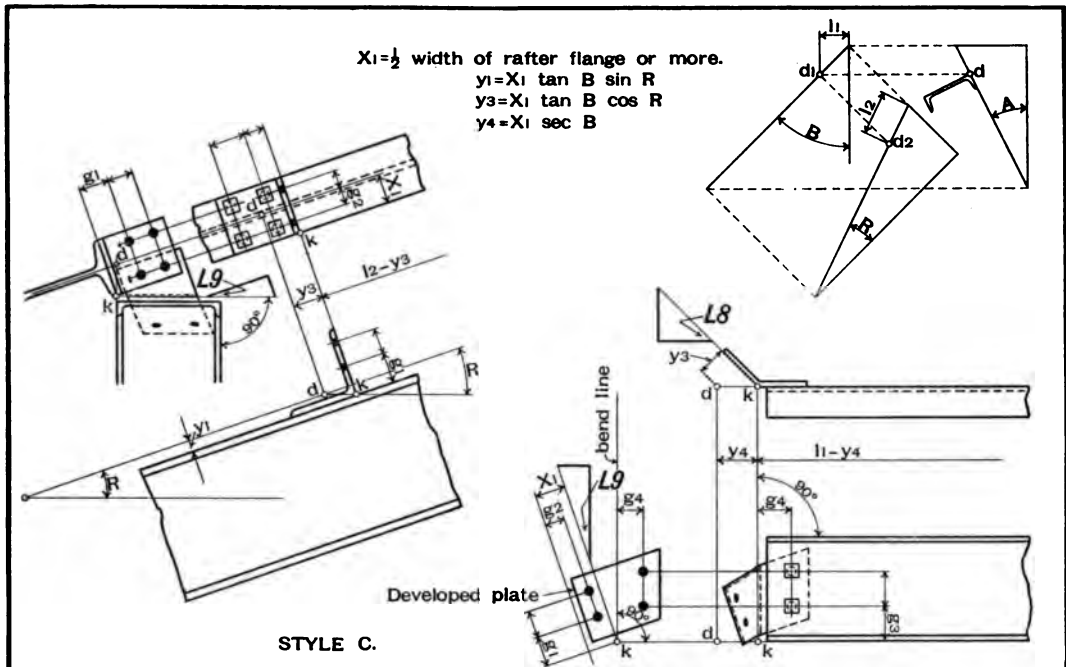
Large Pipe Lines often require both horizontal and vertical change of direction at the same point, which condition may give rise to annoying details. Two separate bends are more expensive and produce greater friction on the flow than a single resultant bend. Careful attention to resultant angles " $X$ " and detail angles " $Y$ " will save much trouble in fabrication and improve the efficiency of the finished structure.

## HIP RAFTER DETAILS

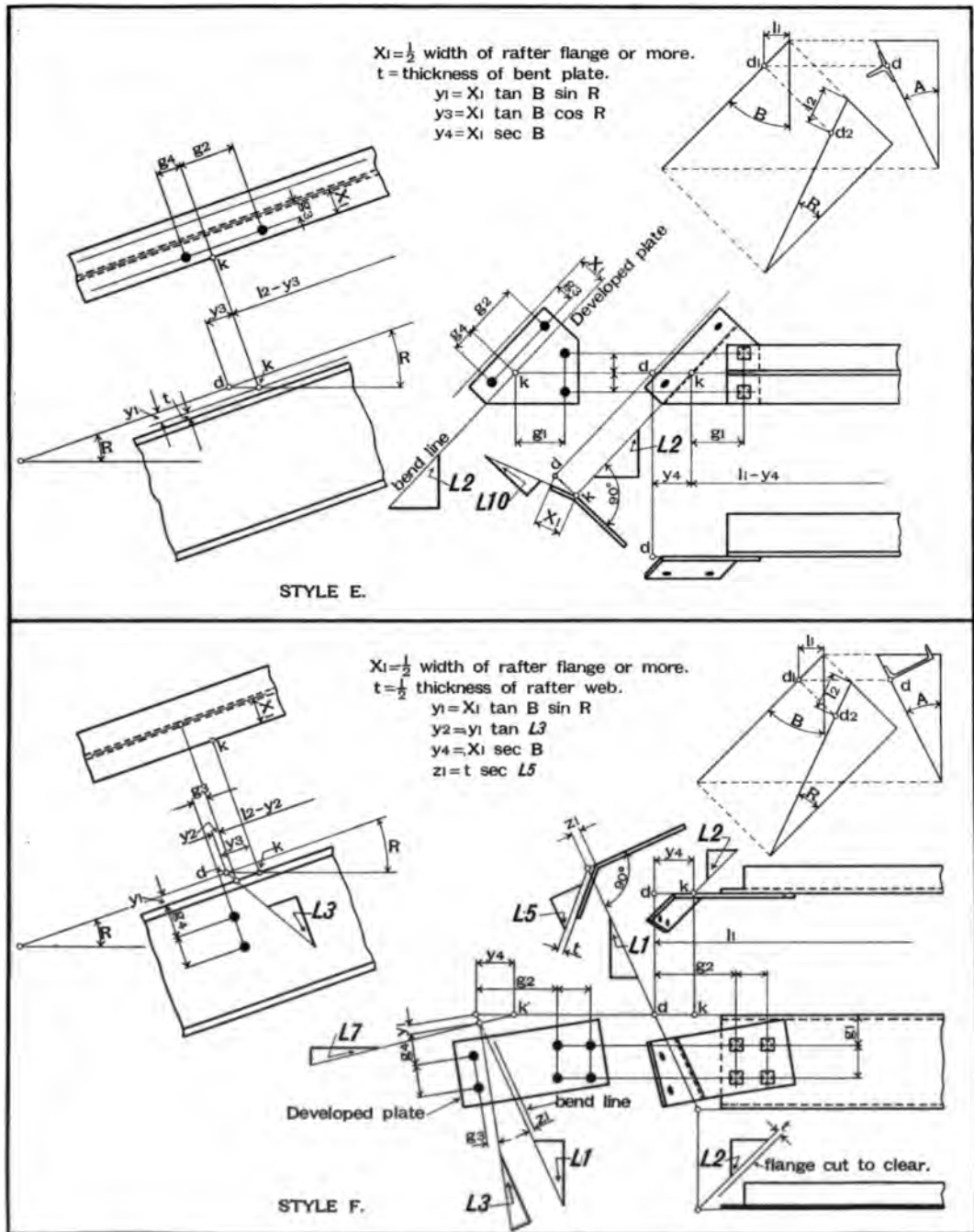




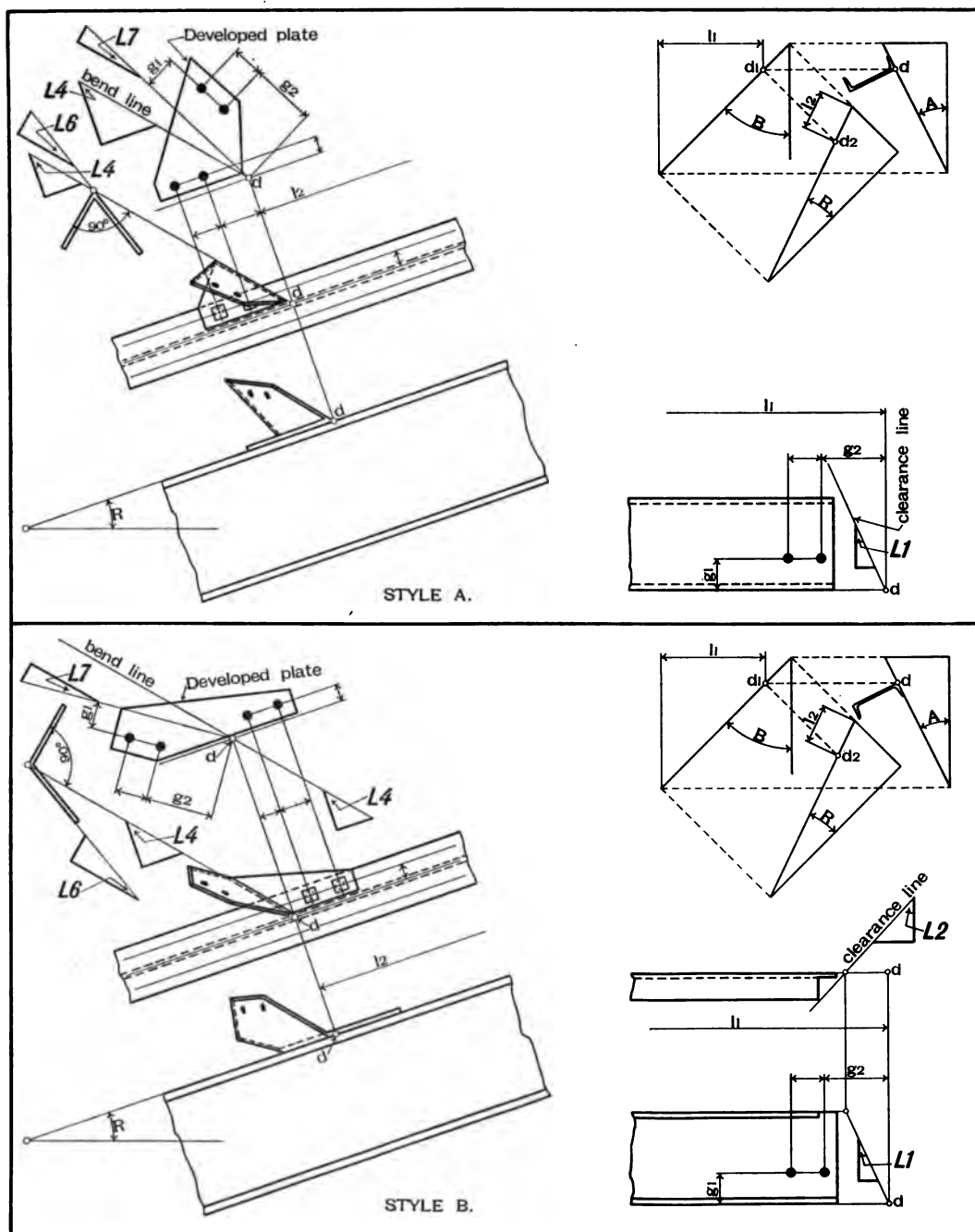
## HIP RAFTER DETAILS



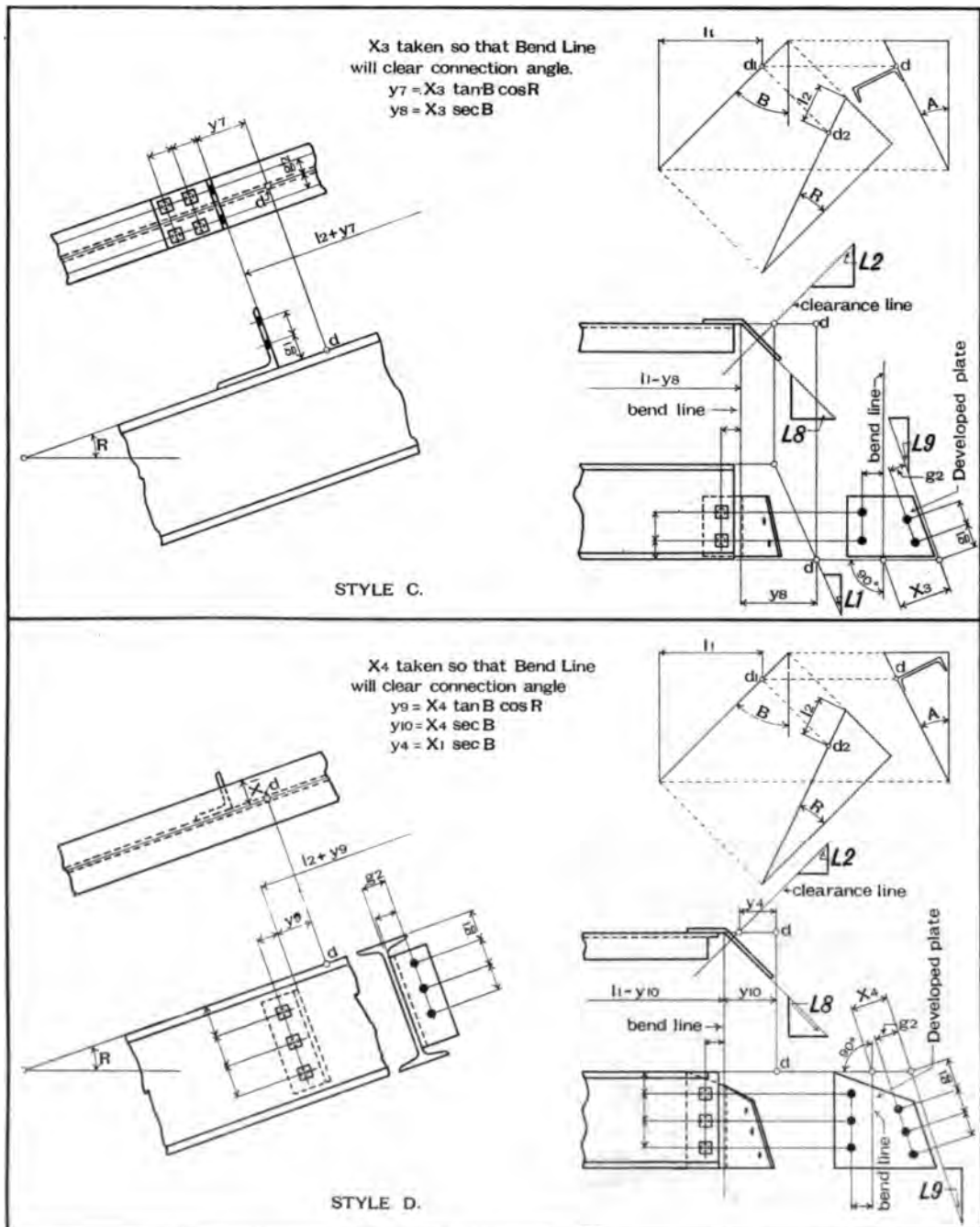
## HIP RAFTER DETAILS



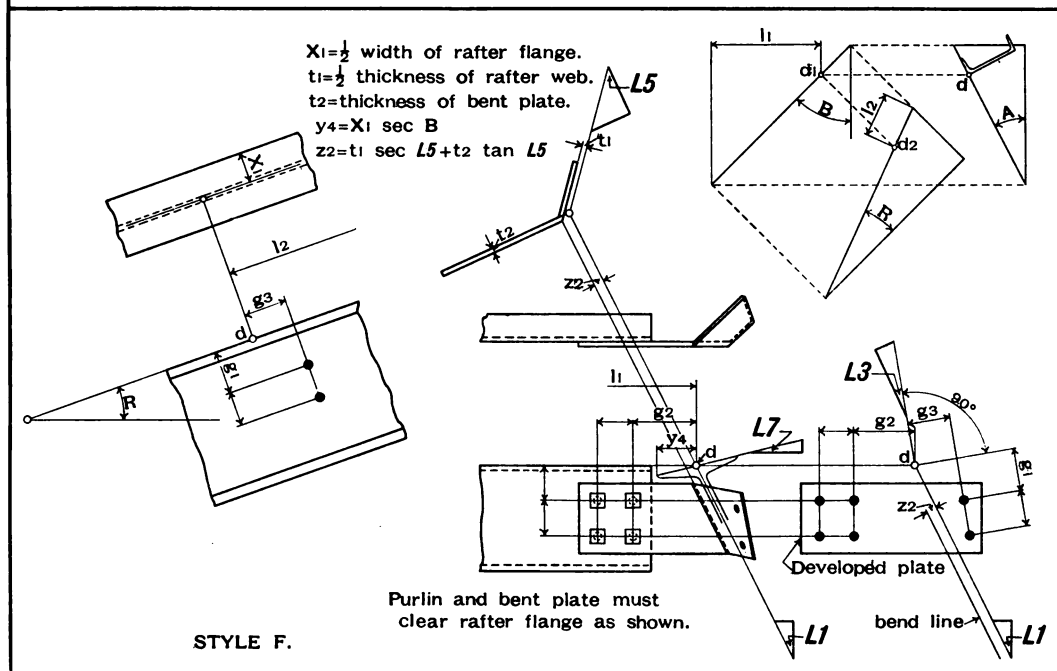
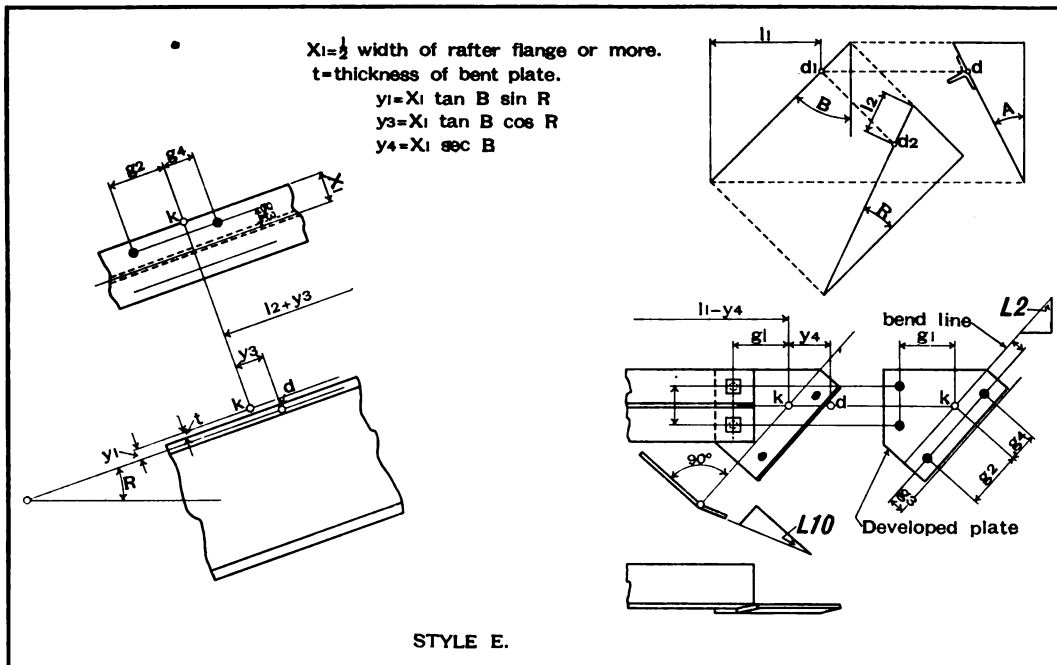
## VALLEY RAFTER DETAILS



# VALLEY RAFTER DETAILS



## VALLEY RAFTER DETAILS





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Seen in Plan as inclined surface  $d_1$ ,  $c_1$ ,  $e_1$ .

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Seen in Elevation of Rafter as surface  $r_2$ ,  $c_2$ ,  $b_2$ .

Seen in Plan as line  $r_1$ ,  $b_1$ .

#### RAFTER FLANGE PLANE.

Seen in Elevation of Rafter as line  $r_2$ ,  $b_2$ .

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$$\tan L5 = \tan L2 \cos L1.$$

$$\tan L7 = \sin A \sin B \cos L4.$$

$$\tan L7 = \cos L2 \tan L10.$$

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# GRAPHIC SOLUTION OF ANGLES

**A = PITCH OF ROOF**

**B = ANGLE BETWEEN TRUSS AND RAFTER IN PLAN**

**R = PITCH OF RAFTER**

$$\tan R = \tan A \cos B$$

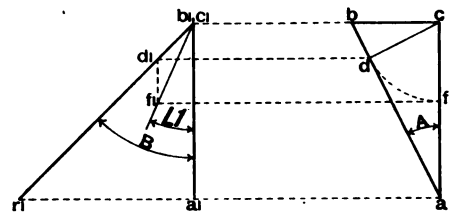
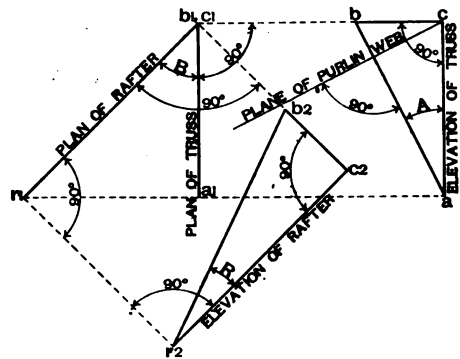
**L1—BEVEL ON PURLIN WEB PLANE MADE BY INTERSECTION OF RAFTER WEB PLANE**

**FORMULA**

$$\tan L1 = \sin A \tan B$$

**GRAPHICS**

- Draw  $d, c \perp a, b$
- Draw  $d, d_1 \parallel b, b_1$
- Revolve  $d$  to  $f$ , about  $c$
- Draw  $f, f_1 \perp d, d_1$
- Draw  $d_1, f_1 \perp d, d_1$
- Connect  $f_1$  with  $c_1$



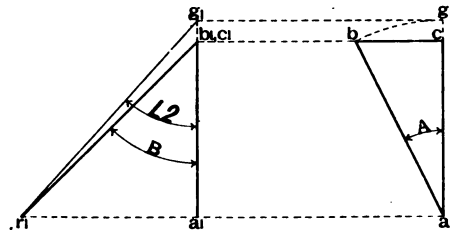
**L2—BEVEL ON ROOF PLANE MADE BY INTERSECTION OF RAFTER WEB PLANE**

**FORMULA**

$$\tan L2 = \tan B \cos A$$

**GRAPHICS**

- Revolve  $b$  to  $g$  about  $a$
- Draw  $g, g_1 \perp b, b_1$
- Extend  $a_1, b_1$  to  $g_1$
- Connect  $g_1$  with  $r_1$



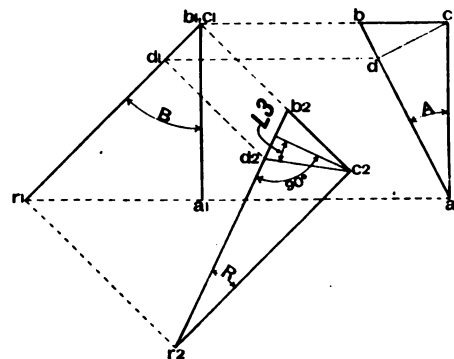
**L3—BEVEL ON RAFTER WEB PLANE MADE BY INTERSECTION OF PURLIN WEB PLANE**

**FORMULA**

$$\tan L3 = \sin A \cos A \sin B \tan B$$

**GRAPHICS**

- Draw  $d, c \perp a, b$
- Draw  $d, d_1 \parallel b, b_1$
- Draw  $d_1, d_2 \perp b_1, b_2$
- Connect  $d_2$  with  $c_2$





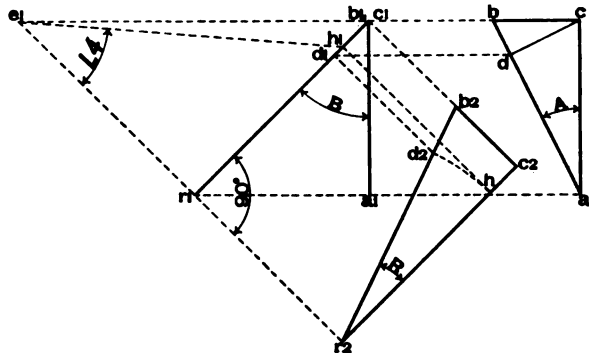
## GRAPHIC SOLUTION OF ANGLES

**L4—BEVEL ON RAFTER FLANGE PLANE MADE BY INTERSECTION OF PURLIN WEB PLANE****FORMULA**

$$\tan L4 = \cos A \tan B \sec R$$

**GRAPHICS**

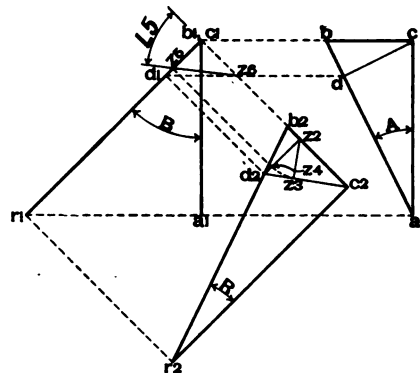
- Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$   
 Draw  $d_1, d_2 \parallel b_1, b_2$   
 Revolve  $d_2$  to  $h$ , about  $r_2$   
 Draw  $h, h_1 \parallel b_1, b_2$   
 Extend  $b, b_1$  to intersect  $r_1, r_2$  at  $e_1$   
 Connect  $e_1$  with  $h_1$

**L5—COMPLEMENT OF ANGLE BETWEEN PURLIN WEB PLANE AND RAFTER WEB PLANE****FORMULA**

$$\tan L5 = \cos L3 \tan L4$$

**GRAPHICS**

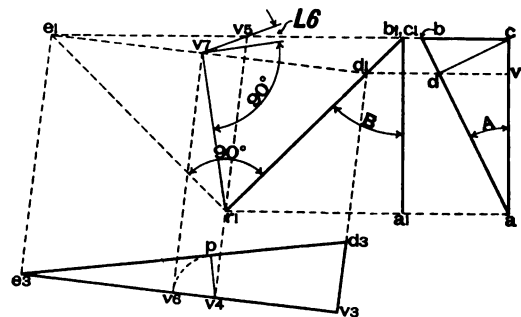
- Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$   
 Draw  $d_1, d_2 \parallel b_1, b_2$   
 Draw  $d_2, z_2 \perp b_2, c_2$   
 Draw  $z_2, z_3 \perp d_2, c_2$   
 Revolve  $z_3$  to  $z_4$  about  $z_2$   
 Draw  $z_4, z_5 \parallel b_1, b_2$   
 Locate  $z_6$  at intersection of  $d, d_1$  and  $c_1, c_2$   
 Connect  $z_5$  with  $z_6$

**L6—COMPLEMENT OF ANGLE BETWEEN PURLIN WEB PLANE AND RAFTER FLANGE PLANE****FORMULA**

$$\tan L6 = \tan L3 \cos L4$$

**GRAPHICS**

- Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$  and extend to  $v$   
 Extend  $b, b_1$  to  $e_1$   
 Connect  $e_1$  with  $d_1$   
 Draw  $e_3, v_3 \parallel e_1, d_1$   
 Draw  $e_1, e_3$  and  $d_1, v_3 \perp e_1, d_1$   
 Take  $v_3, d_3 = d, v$   
 Connect  $e_3$  with  $d_3$   
 Through  $r_1$ , draw  $v_4, v_5 \perp e_1, d_1$   
 Draw  $v_4, p \perp e_3, d_3$   
 Revolve  $p$  to  $v_6$  about  $v_4$   
 Draw  $v_6, v_7 \perp e_1, d_1$   
 Connect  $v_7$  with  $r_1$  and  $v_5$



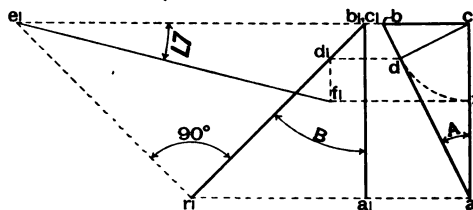
## GRAPHIC SOLUTION OF ANGLES

**L7—BEVEL ON PURLIN WEB PLANE MADE BY RAFTER FLANGE PLANE****FORMULA**

$$\tan L7 = \tan B \sin R \cos L2$$

**GRAPHICS**

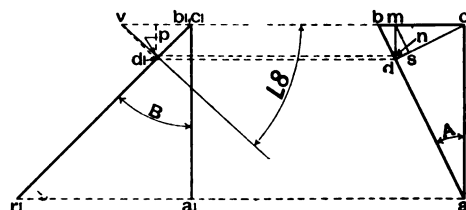
Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$   
 Revolve  $d$  to  $f$  about  $c$   
 Draw  $f, f_1 \parallel b, b_1$   
 Draw  $d_1, f_1 \perp d, d_1$   
 Extend  $b, b_1$  to  $e_1$   
 Connect  $e_1$  with  $f_1$

**L8—ANGLE BETWEEN PURLIN WEB PLANE AND A PLANE PERPENDICULAR TO BOTH RAFTER WEB PLANE AND RAFTER FLANGE PLANE****FORMULA**

$$\tan L8 = \tan B, \cos A$$

**GRAPHICS**

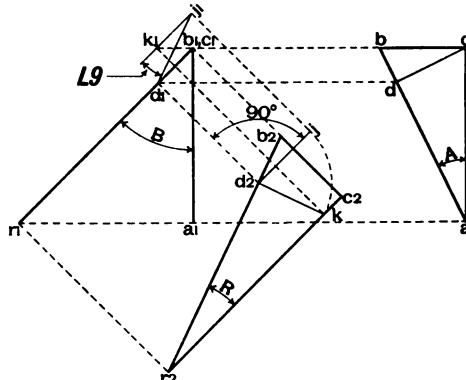
Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$   
 Draw  $d, m \perp b, c$   
 Draw  $m, s \perp d, c$   
 Revolve  $s$  to  $n$  about  $m$   
 Draw  $n, p \parallel d, d_1$   
 Draw  $d_1, p \perp d, d_1$   
 Draw  $d_1, v \perp r_1, b_1$  to intersect  $b, b_1$  at  $v$   
 Connect  $v$  with  $p$

**L9—BEVEL ON PLANE PERPENDICULAR TO BOTH RAFTER WEB PLANE AND RAFTER FLANGE PLANE MADE BY INTERSECTION OF PURLIN WEB PLANE****FORMULA**

$$\tan L9 = \tan B \sin R$$

**GRAPHICS**

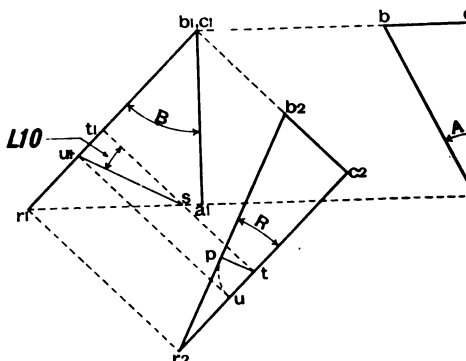
Draw  $d, c \perp a, b$   
 Draw  $d, d_1 \parallel b, b_1$   
 Draw  $d_1, d_2 \parallel b_1, b_2$   
 Draw  $d_2, k \perp r_2, b_2$   
 Draw  $k, k_1 \perp r_1, b_1$   
 Revolve  $k$  to  $j$  about  $d_2$   
 Draw  $j, j_1 \parallel k, k_1$   
 Draw  $k_1, j_1 \perp k, k_1$   
 Connect  $d_1$  with  $j_1$

**L10—ANGLE BETWEEN ROOF PLANE AND RAFTER FLANGE PLANE****FORMULA**

$$\tan L10 = \tan B \sin R$$

**GRAPHICS**

Take  $p$  any point on  $b_2, r_2$   
 Draw  $p, t \perp b_2, r_2$   
 Revolve  $p$  to  $u$  about  $t$   
 Draw  $t, t_1 \parallel b_1, b_2$   
 Draw  $u, u_1 \parallel b_1, b_2$   
 Locate  $s$  at intersection of  $t, t_1$  and  $a, r_1$   
 Connect  $u_1$  with  $s$



## SOLUTIONS, FIVE ORDINARY ROOF PITCHES

B=30°

A	1/5 PITCH		1/4 PITCH		30° PITCH		1/3 PITCH		55° PITCH	
	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.
R	4 $\frac{1}{2}$	9.53959	5 $\frac{1}{4}$	9.63650	6	9.69897	6 $\frac{1}{2}$	9.76144	14 $\frac{27}{32}$	0.09230
L 1	2 $\frac{1}{16}$	9.33127	3 $\frac{3}{32}$	9.41195	3 $\frac{1}{8}$	9.46041	3 $\frac{27}{32}$	9.50550	5 $\frac{1}{16}$	9.67480
L 2	6 $\frac{1}{16}$	9.72921	6 $\frac{1}{16}$	9.71298	6	9.69897	5 $\frac{1}{4}$	9.68159	3 $\frac{21}{32}$	9.52003
L 3	1 $\frac{1}{8}$	8.99801	1 $\frac{13}{32}$	9.06247	1 $\frac{1}{2}$	9.09691	1 $\frac{19}{32}$	9.12462	1 $\frac{1}{8}$	9.13237
L 4	6 $\frac{1}{16}$	9.72159	6 $\frac{1}{32}$	9.70185	5 $\frac{1}{8}$	9.68496	5 $\frac{17}{32}$	9.66421	3 $\frac{1}{8}$	9.48016
L 5	6 $\frac{3}{32}$	9.71945	6	9.69897	5 $\frac{1}{4}$	9.68159	5 $\frac{1}{2}$	9.66039	3 $\frac{1}{16}$	9.47620
L 6	1 $\frac{1}{8}$	8.94484	1 $\frac{1}{4}$	9.01344	1 $\frac{11}{32}$	9.05119	1 $\frac{1}{8}$	9.08268	1 $\frac{1}{16}$	9.11340
L 7	2	9.22157	2 $\frac{1}{16}$	9.30929	2 $\frac{27}{32}$	9.36350	3 $\frac{1}{8}$	9.41532	5 $\frac{1}{4}$	9.62961
L 8	6 $\frac{1}{16}$	9.72921	6 $\frac{1}{16}$	9.71298	6	9.69897	5 $\frac{1}{4}$	9.68159	3 $\frac{21}{32}$	9.52003
L 9	2 $\frac{3}{32}$	9.27642	2 $\frac{1}{4}$	9.36062	3 $\frac{27}{32}$	9.41195	3 $\frac{15}{32}$	9.46041	5 $\frac{1}{8}$	9.65221
L 10	2 $\frac{1}{2}$	9.27642	2 $\frac{1}{4}$	9.36062	3 $\frac{1}{2}$	9.41195	3 $\frac{1}{2}$	9.46041	5 $\frac{1}{8}$	9.65221

"S" = Corresponding Bevels or Slopes to Base of 12 inches.

A	1/5 PITCH				1/4 PITCH				30° PITCH				1/3 PITCH				55° PITCH			
	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>
X 1	1 $\frac{1}{2}$	2 $\frac{1}{2}$	3	4 $\frac{1}{4}$	6 $\frac{1}{4}$	1 $\frac{1}{2}$	2 $\frac{1}{2}$	3	4 $\frac{1}{4}$	6 $\frac{1}{4}$	1 $\frac{1}{2}$	2 $\frac{1}{2}$	3	4 $\frac{1}{4}$	6 $\frac{1}{4}$	1 $\frac{1}{2}$	2 $\frac{1}{2}$	3	4 $\frac{1}{4}$	6 $\frac{1}{4}$
Y 1	$\frac{9}{32}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{32}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{32}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{7}{16}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{32}$
Y 2	$\frac{1}{32}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{16}$
Y 3	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$
Y 4	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$

For Purlins not exceeding 12" Depth, with 4 $\frac{1}{2}$ " Connection Clearance, the following assigned values of X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, give good Results. Y<sub>5</sub> to Y<sub>10</sub> derived therefrom.

## CLEARANCES FOR 9 INCH PURLIN

A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>
	6 $\frac{1}{2}$	5	4 $\frac{1}{2}$	6 $\frac{3}{4}$	5	4 $\frac{1}{2}$	7	5	4 $\frac{1}{2}$	7 $\frac{1}{4}$	5	4 $\frac{1}{2}$	8 $\frac{1}{2}$	5	4 $\frac{1}{2}$
Y 5	3 $\frac{1}{2}$			3 $\frac{1}{4}$			3 $\frac{1}{2}$			3 $\frac{1}{2}$			3 $\frac{1}{2}$		
Y 6	7 $\frac{1}{2}$			7 $\frac{1}{2}$			8 $\frac{1}{2}$			8 $\frac{1}{2}$			9 $\frac{1}{2}$		
Y 7		2 $\frac{27}{32}$			2 $\frac{27}{32}$			2 $\frac{19}{32}$			2 $\frac{1}{2}$			1 $\frac{1}{8}$	
Y 8		5 $\frac{25}{32}$			5 $\frac{25}{32}$			5 $\frac{25}{32}$			5 $\frac{25}{32}$			5 $\frac{25}{32}$	
Y 9			2 $\frac{15}{32}$			2 $\frac{1}{4}$			2 $\frac{1}{4}$			2 $\frac{1}{4}$			1 $\frac{1}{8}$
Y 10			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$

## CLEARANCES FOR 12 INCH PURLIN

A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>
	7	7 $\frac{1}{2}$	4 $\frac{1}{2}$	7 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	8	7 $\frac{1}{2}$	4 $\frac{1}{2}$	8 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	10	7 $\frac{1}{2}$	4 $\frac{1}{2}$
Y 5	3 $\frac{1}{4}$			3 $\frac{1}{4}$			4 $\frac{1}{4}$			4 $\frac{1}{4}$			3 $\frac{1}{4}$		
Y 6	8 $\frac{1}{2}$			8 $\frac{1}{2}$			9 $\frac{1}{4}$			9 $\frac{1}{4}$			11 $\frac{1}{4}$		
Y 7		4 $\frac{3}{32}$			3 $\frac{1}{32}$			3 $\frac{1}{8}$			3 $\frac{1}{8}$			2 $\frac{27}{32}$	
Y 8		8 $\frac{21}{32}$			8 $\frac{21}{32}$			8 $\frac{21}{32}$			8 $\frac{21}{32}$			8 $\frac{21}{32}$	
Y 9			2 $\frac{15}{32}$			2 $\frac{1}{4}$			2 $\frac{1}{4}$			2 $\frac{1}{4}$			1 $\frac{1}{8}$
Y 10			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$			5 $\frac{1}{16}$

## SOLUTIONS, FIVE ORDINARY ROOF PITCHES

**B=45°**

A	1/5 PITCH		1/4 PITCH		30° PITCH		1/3 PITCH		55° PITCH	
	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.
R	3 $\frac{1}{2}$ $\frac{1}{32}$	9.45154	4 $\frac{1}{4}$	9.54845	4 $\frac{7}{8}$	9.61092	5 $\frac{1}{2}$ $\frac{1}{32}$	9.87339	12 $\frac{1}{8}$	0.00426
L 1	4 $\frac{1}{2}$ $\frac{1}{32}$	9.56983	5 $\frac{1}{8}$	9.65051	6	9.69897	6 $\frac{1}{2}$ $\frac{1}{32}$	9.74406	9 $\frac{27}{32}$	9.91336
L 2	11 $\frac{1}{32}$	9.96777	10 $\frac{1}{4}$	9.95154	10 $\frac{13}{32}$	9.93753	10	9.92015	6 $\frac{1}{8}$	9.75859
L 3	2 $\frac{1}{2}$ $\frac{1}{16}$	9.38709	3 $\frac{3}{8}$	9.45154	3 $\frac{1}{2}$ $\frac{1}{16}$	9.48599	3 $\frac{29}{32}$	9.51369	4	9.52144
L 4	10 $\frac{1}{4}$	9.95225	10 $\frac{9}{16}$	9.92867	9 $\frac{29}{32}$	9.90853	9 $\frac{9}{16}$	9.88387	5 $\frac{5}{8}$	9.66984
L 5	10 $\frac{7}{16}$	9.93971	9 $\frac{1}{4}$ $\frac{1}{16}$	9.91195	9 $\frac{1}{16}$	9.88908	8 $\frac{29}{32}$	9.86190	5 $\frac{1}{16}$	9.64710
L 6	2 $\frac{3}{16}$	9.25914	2 $\frac{1}{8}$ $\frac{1}{32}$	9.33379	2 $\frac{7}{16}$	9.37641	3 $\frac{1}{8}$	9.41357	3 $\frac{3}{8}$	9.47851
L 7	2 $\frac{1}{2}$ $\frac{1}{32}$	9.29984	2 $\frac{1}{2}$ $\frac{1}{32}$	9.39524	3 $\frac{1}{16}$	9.45593	3 $\frac{1}{2}$ $\frac{1}{16}$	9.51568	7 $\frac{1}{8}$ $\frac{1}{32}$	9.78984
L 8	11 $\frac{1}{32}$	9.96777	10 $\frac{1}{4}$	9.95154	10 $\frac{13}{32}$	9.93753	10	9.92015	6 $\frac{1}{8}$	9.75859
L 9	3 $\frac{1}{4}$	9.43483	4	9.52288	4 $\frac{1}{2}$ $\frac{1}{32}$	9.57745	5 $\frac{1}{8}$	9.62982	8 $\frac{1}{2}$ $\frac{1}{32}$	9.85160
L 10	3 $\frac{1}{4}$	9.43483	4	9.52288	4 $\frac{1}{2}$ $\frac{1}{32}$	9.57745	5 $\frac{1}{8}$	9.62982	8 $\frac{1}{2}$ $\frac{1}{32}$	9.85160

"S" — Corresponding Bevels or Slopes to Base of 12 inches.

A	1/5 PITCH				1/4 PITCH				30° PITCH				1/3 PITCH				55° PITCH			
	X	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
X 1	1 $\frac{1}{2}$	2 $\frac{1}{2}$	3	4 $\frac{1}{4}$	5 $\frac{1}{4}$	6 $\frac{1}{4}$	7 $\frac{1}{4}$	8 $\frac{1}{4}$	9 $\frac{1}{4}$	10 $\frac{1}{4}$	11 $\frac{1}{4}$	12 $\frac{1}{4}$	13 $\frac{1}{4}$	14 $\frac{1}{4}$	15 $\frac{1}{4}$	16 $\frac{1}{4}$	17 $\frac{1}{4}$	18 $\frac{1}{4}$	19 $\frac{1}{4}$	20 $\frac{1}{4}$
Y 1	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$
Y 2	1 $\frac{1}{4}$	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$	6
Y 3	1 $\frac{3}{8}$	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$	6
Y 4	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$	6	6 $\frac{1}{4}$

For Purlins not exceeding 12" Depth, with 4 $\frac{1}{2}$ " Connection Clearance, the following assigned values of X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub> give good Results. Y<sub>5</sub> to Y<sub>10</sub> derived therefrom.

## CLEARANCES FOR 9 INCH PURLIN

A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =
	7	5 $\frac{1}{2}$	4 $\frac{1}{2}$	7 $\frac{1}{2}$	5 $\frac{1}{2}$	4 $\frac{1}{2}$	8	5 $\frac{1}{2}$	4 $\frac{1}{2}$	8 $\frac{1}{2}$	5 $\frac{1}{2}$	4 $\frac{1}{2}$	10	5 $\frac{1}{2}$	4 $\frac{1}{2}$
Y 5	6 $\frac{1}{4}$			7 $\frac{1}{8}$			7 $\frac{1}{8}$			7 $\frac{1}{8}$			7 $\frac{1}{8}$		
Y 6	9 $\frac{27}{32}$			10 $\frac{1}{32}$			11 $\frac{1}{16}$			12 $\frac{1}{32}$			14 $\frac{1}{32}$		
Y 7		5 $\frac{9}{32}$			5 $\frac{9}{32}$			5 $\frac{9}{32}$			4 $\frac{31}{32}$			3 $\frac{7}{8}$	
Y 8		7 $\frac{25}{32}$			7 $\frac{25}{32}$			7 $\frac{25}{32}$			7 $\frac{25}{32}$			7 $\frac{25}{32}$	
Y 9			4 $\frac{1}{32}$			4 $\frac{1}{32}$			4 $\frac{1}{32}$			4 $\frac{1}{32}$			3 $\frac{3}{32}$
Y 10			6 $\frac{1}{8}$			6 $\frac{1}{8}$			6 $\frac{1}{8}$			6 $\frac{1}{8}$			6 $\frac{1}{8}$

## CLEARANCES FOR 12 INCH PURLIN

A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =
	8	7 $\frac{1}{2}$	4 $\frac{1}{2}$	8 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	9	7 $\frac{1}{2}$	4 $\frac{1}{2}$	9 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	11 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$
Y 5	7 $\frac{1}{16}$			8			8 $\frac{1}{16}$			8 $\frac{1}{16}$			8 $\frac{1}{16}$		
Y 6	11 $\frac{1}{16}$			12 $\frac{1}{16}$			12 $\frac{1}{16}$			13 $\frac{1}{16}$			16 $\frac{1}{16}$		
Y 7		7 $\frac{1}{16}$			7 $\frac{1}{16}$			6 $\frac{1}{16}$			6 $\frac{1}{16}$			5 $\frac{1}{16}$	
Y 8		10 $\frac{1}{16}$			10 $\frac{1}{16}$			10 $\frac{1}{16}$			10 $\frac{1}{16}$			10 $\frac{1}{16}$	
Y 9			4 $\frac{1}{16}$			4 $\frac{1}{16}$			4 $\frac{1}{16}$			4 $\frac{1}{16}$			3 $\frac{1}{16}$
Y 10			6 $\frac{1}{16}$			6 $\frac{1}{16}$			6 $\frac{1}{16}$			6 $\frac{1}{16}$			6 $\frac{1}{16}$

## SOLUTIONS, FIVE ORDINARY ROOF PITCHES

**B=50°**

A	1/5 PITCH		1/4 PITCH		30° PITCH		1/3 PITCH		55° PITCH	
	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.	"S"	Log. Tan.
R	3 $\frac{1}{2}$ <sub>32</sub>	9.41013	3 $\frac{27}{32}$	9.50704	4 $\frac{15}{32}$	9.56951	5 $\frac{7}{32}$	9.63198	11	9.96284
L 1	5 $\frac{1}{16}$	9.64602	6 $\frac{1}{32}$	9.72670	7 $\frac{9}{32}$	9.77516	7 $\frac{15}{16}$	9.82024	11 $\frac{27}{32}$	9.98955
L 2	13 $\frac{9}{32}$	0.04396	12 $\frac{27}{32}$	0.02773	12 $\frac{3}{8}$	0.01372	11 $\frac{27}{32}$	9.99634	8 $\frac{7}{16}$	9.83478
L 3	3 $\frac{27}{32}$	9.49804	4 $\frac{3}{8}$	9.56250	4 $\frac{3}{4}$	9.59694	5 $\frac{1}{16}$	9.62465	5 $\frac{5}{32}$	9.63240
L 4	12 $\frac{27}{32}$	0.02563	12 $\frac{1}{32}$	0.00062	11 $\frac{7}{16}$	9.97927	10 $\frac{27}{32}$	9.95309	6 $\frac{3}{8}$	9.72610
L 5	12 $\frac{3}{32}$	0.00511	11 $\frac{9}{32}$	9.97344	10 $\frac{5}{8}$	9.94775	9 $\frac{15}{16}$	9.91761	5 $\frac{7}{8}$	9.68942
L 6	21 $\frac{9}{32}$	9.33433	3 $\frac{7}{16}$	9.41167	3 $\frac{7}{16}$	9.45655	3 $\frac{3}{4}$	9.49632	4 $\frac{17}{32}$	9.57824
L 7	2 $\frac{3}{8}$	9.29881	3	9.39706	3 $\frac{1}{2}$	9.46025	4	9.52286	8	9.82305
L 8	13 $\frac{9}{32}$	0.04396	12 $\frac{27}{32}$	0.02773	12 $\frac{3}{8}$	0.01372	11 $\frac{27}{32}$	9.99634	8 $\frac{7}{16}$	9.83478
L 9	3 $\frac{7}{16}$	9.47241	4 $\frac{3}{8}$	9.56188	4 $\frac{21}{32}$	9.61767	5 $\frac{3}{8}$	9.67155	9 $\frac{27}{32}$	9.90630
L 10	3 $\frac{7}{16}$	9.47241	4 $\frac{3}{8}$	9.56188	4 $\frac{21}{32}$	9.61767	5 $\frac{3}{8}$	9.67155	9 $\frac{27}{32}$	9.90630

"S"—Corresponding Bevels or Slopes to Base of 12 inches.

A	1/5 PITCH						1/4 PITCH						30° PITCH						1/3 PITCH						55° PITCH					
	X 1	1½	2½	3	4¼	6¼	1½	2½	3	4¼	6¼	1½	2½	3	4¼	6¼	1½	2½	3	4¼	6¼	1½	2½	3	4¼	6¼				
Y 1	1 <sup>7</sup> / <sub>16</sub>	¾	2 <sup>3</sup> / <sub>8</sub>	1¼	1 <sup>1</sup> / <sub>2</sub>	1 <sup>7</sup> / <sub>8</sub>	1 <sup>9</sup> / <sub>16</sub>	2 <sup>3</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>4</sub>	1 <sup>1</sup> / <sub>2</sub>	2 <sup>3</sup> / <sub>8</sub>	5 <sup>8</sup> / <sub>16</sub>	1 <sup>1</sup> / <sub>2</sub>	1¼	1 <sup>3</sup> / <sub>4</sub>	2 <sup>3</sup> / <sub>8</sub>	2 <sup>3</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	2	2 <sup>1</sup> / <sub>8</sub>	1 <sup>7</sup> / <sub>8</sub>	2	2 <sup>3</sup> / <sub>8</sub>	3 <sup>7</sup> / <sub>8</sub>	5 <sup>1</sup> / <sub>8</sub>				
Y 2	3 <sup>5</sup> / <sub>16</sub>	¾	3 <sup>3</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	2 <sup>3</sup> / <sub>8</sub>	¾	1 <sup>1</sup> / <sub>8</sub>	½	1 <sup>1</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	1 <sup>5</sup> / <sub>8</sub>	1 <sup>3</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>8</sub>	2	2 <sup>1</sup> / <sub>8</sub>	1 <sup>7</sup> / <sub>8</sub>	2	2 <sup>3</sup> / <sub>8</sub>	3 <sup>7</sup> / <sub>8</sub>	5 <sup>1</sup> / <sub>8</sub>				
Y 3	1 <sup>1</sup> / <sub>8</sub>	2 <sup>7</sup> / <sub>8</sub>	3 <sup>1</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	7 <sup>7</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>2</sub>	2 <sup>7</sup> / <sub>8</sub>	3 <sup>1</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	7 <sup>7</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>2</sub>	2 <sup>7</sup> / <sub>8</sub>	3 <sup>1</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	7 <sup>7</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>2</sub>	2 <sup>7</sup> / <sub>8</sub>	3 <sup>1</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	7 <sup>7</sup> / <sub>8</sub>	1 <sup>1</sup> / <sub>2</sub>	2 <sup>7</sup> / <sub>8</sub>	3 <sup>1</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	7 <sup>7</sup> / <sub>8</sub>					
Y 4	2 <sup>1</sup> / <sub>8</sub>	3 <sup>7</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	6 <sup>5</sup> / <sub>8</sub>	9 <sup>3</sup> / <sub>8</sub>	2 <sup>1</sup> / <sub>2</sub>	3 <sup>7</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	6 <sup>5</sup> / <sub>8</sub>	9 <sup>3</sup> / <sub>8</sub>	2 <sup>1</sup> / <sub>2</sub>	3 <sup>7</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	6 <sup>5</sup> / <sub>8</sub>	9 <sup>3</sup> / <sub>8</sub>	2 <sup>1</sup> / <sub>2</sub>	3 <sup>7</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	6 <sup>5</sup> / <sub>8</sub>	9 <sup>3</sup> / <sub>8</sub>	2 <sup>1</sup> / <sub>2</sub>	3 <sup>7</sup> / <sub>8</sub>	4 <sup>1</sup> / <sub>8</sub>	6 <sup>5</sup> / <sub>8</sub>	9 <sup>3</sup> / <sub>8</sub>					

For Purlins not exceeding 12" Depth, with 4 $\frac{1}{4}$ " Connection Clearance, the following assigned values of X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, give good results. Y<sub>5</sub> to Y<sub>10</sub> derived therefrom.

## CLEARANCES FOR 9 INCH PURLIN

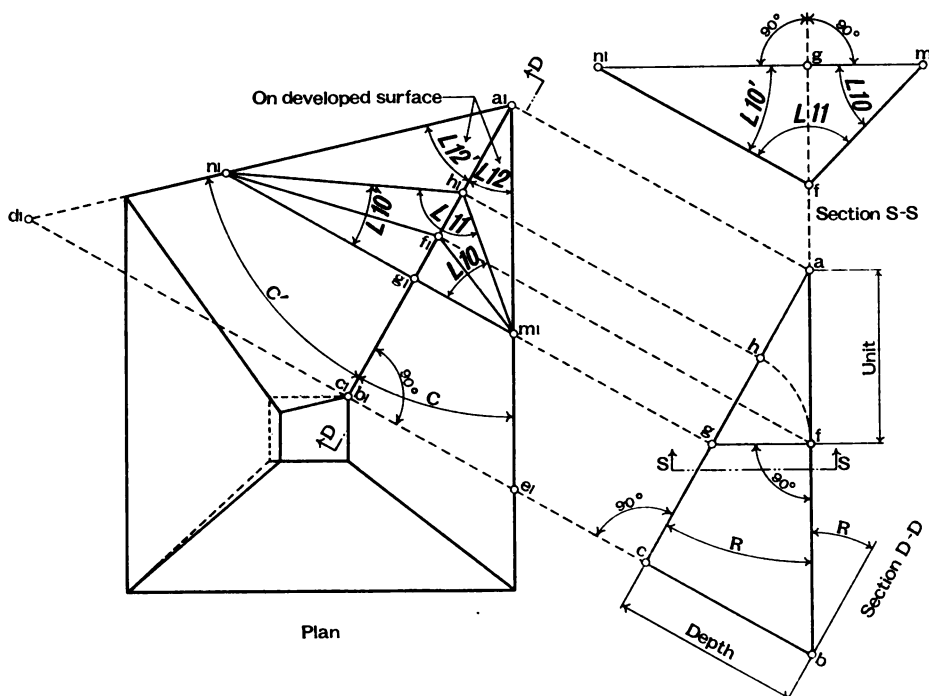
A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =
	7 $\frac{1}{2}$	5 $\frac{1}{2}$	4 $\frac{1}{2}$	8	5 $\frac{1}{2}$	4 $\frac{1}{2}$	8 $\frac{1}{2}$	5 $\frac{1}{2}$	4 $\frac{1}{2}$	9	5 $\frac{1}{2}$	4 $\frac{1}{2}$	10 $\frac{1}{2}$	5 $\frac{1}{2}$	4 $\frac{1}{2}$
Y 5	8 $\frac{1}{2}$	.....	.....	9 $\frac{1}{2}$	.....	.....	9 $\frac{1}{2}$	.....	.....	9 $\frac{27}{32}$	.....	.....	9 $\frac{7}{32}$	.....	.....
Y 6	11 $\frac{27}{32}$	.....	.....	12 $\frac{7}{16}$	.....	.....	13 $\frac{7}{32}$	.....	.....	14	.....	.....	16 $\frac{11}{32}$	.....	.....
Y 7	.....	6 $\frac{1}{32}$	.....	.....	6 $\frac{1}{8}$	.....	.....	6 $\frac{9}{32}$	.....	.....	6 $\frac{1}{32}$	.....	.....	4 $\frac{27}{32}$	.....
Y 8	.....	8 $\frac{1}{16}$	.....	.....	8 $\frac{1}{16}$	.....	.....	8 $\frac{1}{16}$	.....	.....	8 $\frac{1}{16}$	.....	.....	8 $\frac{1}{16}$	.....
Y 9	.....	.....	5 $\frac{1}{16}$	.....	.....	5 $\frac{9}{32}$	.....	5 $\frac{1}{32}$	.....	.....	.....	4 $\frac{15}{16}$	.....	.....	3 $\frac{15}{16}$
Y 10	.....	.....	7	.....	.....	7	.....	7	.....	.....	.....	7	.....	.....	7

## CLEARANCES FOR 12 INCH PURLIN

A	1/5 PITCH			1/4 PITCH			30° PITCH			1/3 PITCH			55° PITCH		
	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =	X <sub>2</sub> =	X <sub>3</sub> =	X <sub>4</sub> =
	8 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	9	7 $\frac{1}{2}$	4 $\frac{1}{2}$	9 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$	10	7 $\frac{1}{2}$	4 $\frac{1}{2}$	12 $\frac{1}{2}$	7 $\frac{1}{2}$	4 $\frac{1}{2}$
Y 5	9 $\frac{15}{16}$	.....	.....	10 $\frac{7}{32}$	.....	.....	10 $\frac{5}{8}$	.....	.....	10 $\frac{21}{32}$	.....	.....	10 $\frac{11}{32}$	.....	.....
Y 6	13 $\frac{7}{32}$	.....	.....	14	.....	.....	14 $\frac{25}{32}$	.....	.....	15 $\frac{9}{16}$	.....	.....	19 $\frac{1}{16}$	.....	.....
Y 7	.....	8 $\frac{21}{32}$	.....	.....	8 $\frac{1}{2}$	.....	.....	8 $\frac{3}{8}$	.....	.....	8 $\frac{7}{32}$	.....	.....	6 $\frac{1}{8}$	.....
Y 8	.....	11 $\frac{21}{32}$	.....	.....	11 $\frac{21}{32}$	.....	.....	11 $\frac{21}{32}$	.....	.....	11 $\frac{21}{32}$	.....	.....	11 $\frac{21}{32}$	.....
Y 9	.....	.....	5 $\frac{1}{16}$	.....	.....	5 $\frac{9}{32}$	.....	5 $\frac{1}{32}$	.....	.....	.....	4 $\frac{15}{16}$	.....	.....	3 $\frac{15}{16}$
Y 10	.....	.....	7	.....	.....	7	.....	7	.....	.....	.....	7	.....	.....	7

# HOPPERS, BINS AND CHUTES

## FORMULAE AND GRAPHICS FOR SOLUTION OF ANGLES



### EXPLANATION

Inclined surfaces  $a_1, b_1, e_1$ , and  $a_1, b_1, d_1$ , intersect on line  $a_1, b_1$ , forming dihedral angle measured by angle  $L11$ . (See Section S-S.)

Vertical section  $a, b, c$ , (Section D-D) divides the dihedral into two dihedrals, of which  $L10$  and  $L10'$  are respectively the complements.

Angles  $R, C$  and  $C'$  must be determined from design.

Rectangular oottom with irregular top will produce slightly warped side surfaces, see dotted lines for this condition.

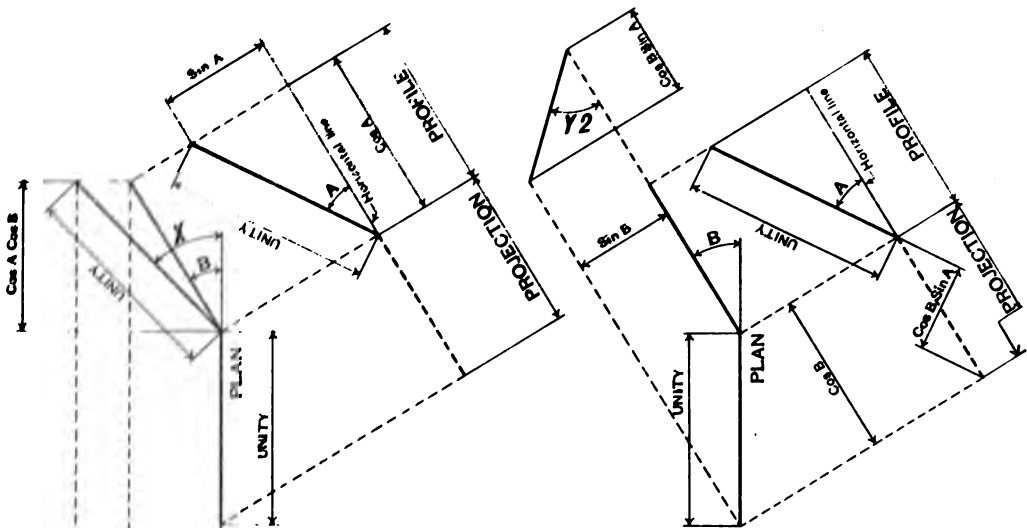
#### GRAPHICS

Choose any point  $f$  in line  $a, b$   
 Draw  $f, g, i$   $\perp$   $a, b$   
 Draw  $g, n_1 \perp a, c$   
 Project  $f$  to  $f_1$  in plan  
 Draw  $f_1, m_1$  and  $f_1, n_1$  in plan  
 Then  $m_1, n_1, f_1$  is plan of Section S-S  
 Revolve  $f$  to  $h$  about  $g$   
 Project  $h$  to  $h_1$  in plan  
 Draw  $h_1, m_1$ , and  $h_1, n_1$   
 Then  $h_1, m_1, n_1$  is true view of Section S-S

#### FORMULAE

$\tan L10 = \sin R \cot C$   
 $\tan L10' = \sin R \cot C'$   
 $L11 = 180^\circ - (L10 + L10')$   
 $\tan L12 = \sec R \tan C \sec L10$   
 $\tan L12' = \sec R \tan C' \sec L10'$   
 $\cos L12 = \cos R \cos C$   
 $\cos L12' = \cos R \cos C'$

# PIPE CONNECTION, RESULTANT OF TWO BENDS



## NOTES:—

### KNOWN ANGLES:—

Angle A in plane of profile

Angle B in horizontal plane or plan

THE PROFILE is the vertical section taken thru the center of the pipe line

THE LINE P-P is perpendicular to center line of pipe in plane of profile

### ANGLES TO BE SOLVED:—

Resultant Angle X

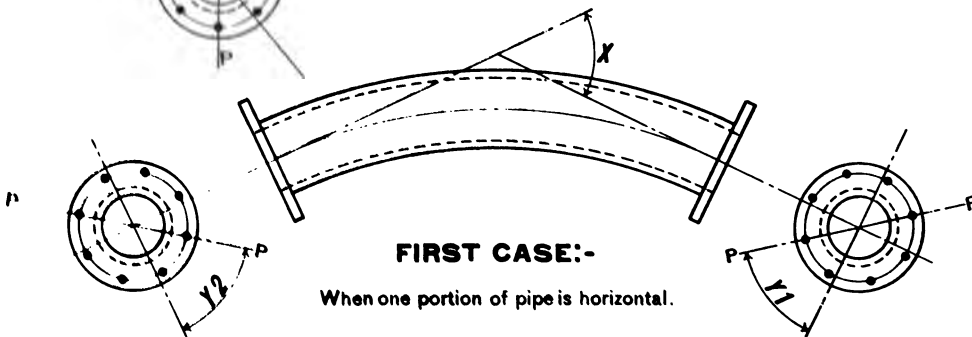
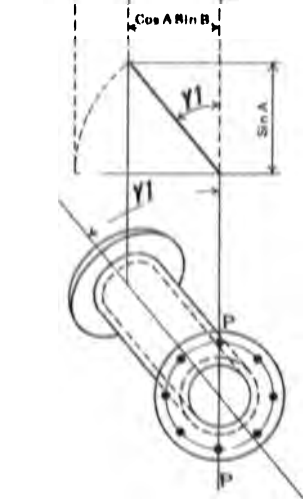
Detail Angles Y1 and Y2

### FORMULAE:—

$$\cos X = \cos A \cos B$$

$$\tan Y1 = \frac{\cos A \sin B}{\sin A} - \cot A \sin B$$

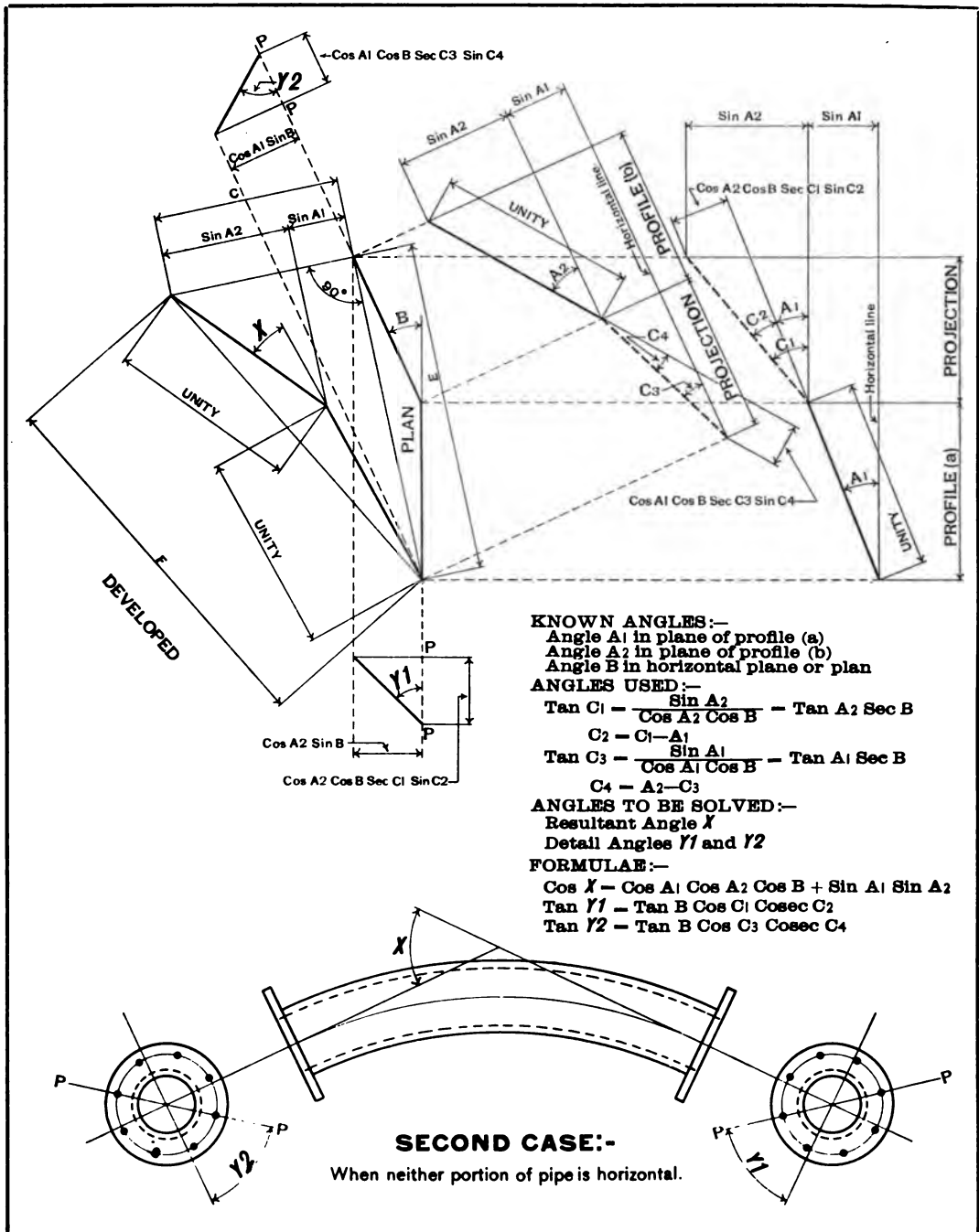
$$\tan Y2 = \frac{\sin B}{\cos B \sin A} - \tan B \operatorname{cosec} A$$



## FIRST CASE:—

When one portion of pipe is horizontal.

# PIPE CONNECTION, RESULTANT OF TWO BENDS







## ANALYTIC PROOFS

Refer to Page 10; a c=unity.

## Tangent R

$$\begin{aligned}
 \text{Tan } R &= \frac{cs, b_2}{cs, r_2} \\
 cs, b_2 &= c, b \\
 &= \text{Tan } A \\
 cs, r_2 &= d, r_1 \\
 &= \text{Sec } B \\
 \therefore \text{Tan } R &= \frac{\text{Tan } A}{\text{Sec } B} \\
 &= \text{Tan } A \cos B \quad \checkmark
 \end{aligned}$$

## Tangent L1

$$\begin{aligned}
 \text{Tan } L1 &= \frac{f_1, z_1}{f, c} \\
 f_1, z_1 &= d_1, z_2 \\
 &= (d, m) \text{ Tan } B \\
 \text{But } d, m &= \text{Sin}^2 A \\
 \therefore f_1, z_1 &= \text{Sin}^2 A \text{ Tan } B \\
 f, c &= d, c \\
 &= \text{Sin } A \\
 \therefore \text{Tan } L1 &= \frac{\text{Sin}^2 A \text{ Tan } B}{\text{Sin } A} \\
 &= \text{Sin } A \text{ Tan } B
 \end{aligned}$$

## Tangent L2

$$\begin{aligned}
 \text{Tan } L2 &= \frac{g_1, z_3}{b, g} \\
 g_1, z_3 &= d_1, z_2 \\
 &= (d, m) \text{ Tan } B \\
 \text{But } d, m &= \text{Sin}^2 A \\
 \therefore g_1, z_3 &= \text{Sin}^2 A \text{ Tan } B \\
 b, g &= b, d \\
 &= (d, c) \text{ Tan } A \\
 &= \text{Sin } A \text{ Tan } A \\
 \therefore \text{Tan } L2 &= \frac{\text{Sin}^2 A \text{ Tan } B}{\text{Sin } A \text{ Tan } A} \\
 &= \frac{\text{Sin } A \text{ Tan } B}{\text{Tan } A} \\
 &= \text{Cos } A \text{ Tan } B
 \end{aligned}$$

## Tangent L4

$$\begin{aligned}
 \text{Tan } L4 &= \frac{r_1, h_1}{r_1, e_1} \\
 r_1, h_1 &= r_2, h \\
 &= r_2, d_2 \\
 &= \text{Cos}^2 A \text{ Sec } B \text{ Sec } R \\
 r_1, e_1 &= \text{Osc } B \\
 \therefore \text{Tan } L4 &= \frac{\text{Cos}^2 A \text{ Sec } B \text{ Sec } R}{\text{Osc } B} \\
 &= \frac{\text{Cos}^2 A \text{ Sin } B}{\text{Cos } B \text{ Cos } R} \\
 &= \text{Cos}^2 A \text{ Tan } B \text{ Sec } R
 \end{aligned}$$

## Tangent L7

$$\begin{aligned}
 \text{Tan } L7 &= \frac{f_1, k_1}{e_1, k_1} \\
 f_1, k_1 &= c, f \\
 &= d, c \\
 &= \text{Sin } A \\
 a, d &= \text{Cos } A \\
 r_2, d_2 &= (a, d) \text{ Sec } L2 \\
 &= \text{Cos } A \text{ Sec } L2 \\
 r_2, k_1 &= (r_2, d_2) \text{ Sec } R \\
 &= \text{Cos } A \text{ Sec } L2 \text{ Sec } R \\
 e_1, k_1 &= (r_2, k) \text{ Osc } B \\
 &= \text{Cos } A \text{ Sec } L2 \text{ Sec } R \text{ Osc } B \\
 \therefore \text{Tan } L7 &= \frac{\text{Sin } A}{\text{Cos } A \text{ Sec } L2 \text{ Sec } R \text{ Osc } B} \\
 &= \text{Tan } A \text{ Cos } L2 \text{ Cos } R \text{ Sin } B \\
 &= \text{Tan } A \left( \frac{\text{Sin } R}{\text{Tan } R} \right) \text{ Tan } B \text{ Cos } B \text{ Cos } L2 \\
 &= \frac{\text{Tan } A \text{ Sin } R \text{ Tan } B \text{ Cos } B \text{ Cos } L2}{\text{Tan } A \text{ Cos } B} \\
 &= \text{Sin } R \text{ Tan } B \text{ Cos } L2
 \end{aligned}$$

## Tangent L8

$$\begin{aligned}
 \text{Tan } L8 &= \frac{n_1, k_1}{k_1, v} \\
 n_1, k_1 &= n, m \\
 &= m, w \\
 &= (d, m) \text{ Cos } A \\
 &= \text{Sin}^2 A \text{ Cos } A \\
 k_1, v &= (d_1, k_1) \text{ Cot } B \\
 &= (d, m) \text{ Cot } B \\
 &= \text{Sin}^2 A \text{ Cot } B \\
 \therefore \text{Tan } L8 &= \frac{\text{Sin}^2 A \text{ Cos } A}{\text{Sin}^2 A \text{ Cot } B} \\
 &= \text{Cos } A \text{ Tan } B
 \end{aligned}$$

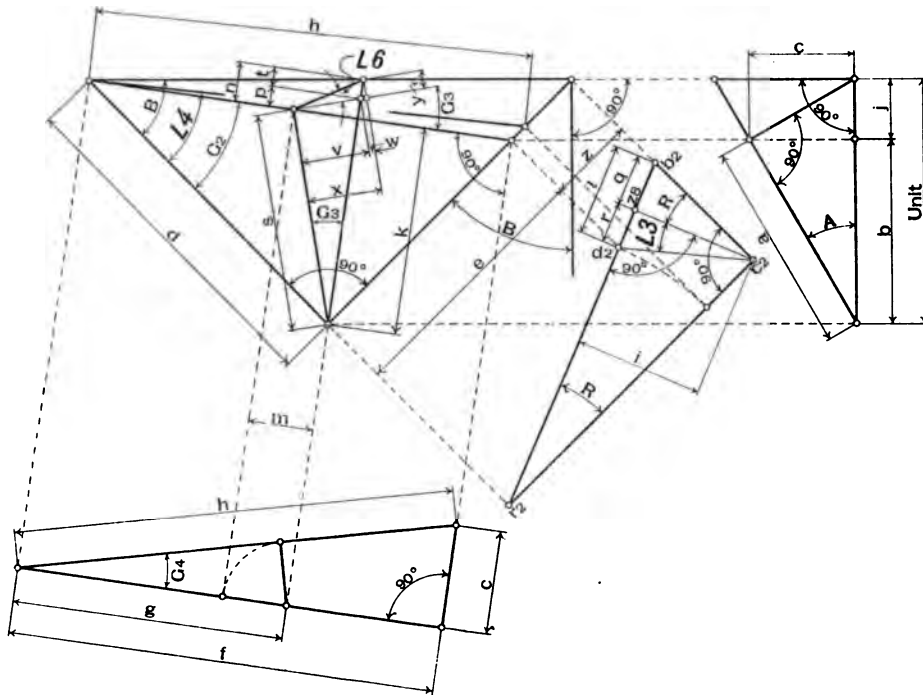
## Tangent L9

$$\begin{aligned}
 \text{Tan } L9 &= \frac{j_1, z_4}{d_1, z_4} \\
 d_1, z_4 &= d_2, j \\
 &= d_2, k \\
 j_1, z_4 &= k_1, z_6 \\
 &= (d_1, z_6) \text{ Tan } B \\
 d_1, z_6 &= (d_2, k) \text{ Sin } R \\
 \therefore j_1, z_4 &= (d_2, k) \text{ Sin } R \text{ Tan } B \\
 \therefore \text{Tan } L9 &= \frac{(d_2, k) \text{ Sin } R \text{ Tan } B}{(d_2, k)} \\
 &= \text{Sin } R \text{ Tan } B
 \end{aligned}$$

## Tangent L10

$$\begin{aligned}
 \text{Tan } L10 &= \frac{u_1, t_1}{t_1, s_1} \\
 p \text{ is any point on } r_2, b_2 \\
 \text{Choose location such that } s_1 \text{ will fall at } a \\
 t_1, s_1 &= \text{Sin } B \\
 t, r_2 &= t_1, r_1 \\
 &= (r_1, s_1) \text{ Sin } B \\
 &= \text{Tan } B \text{ Sin } B \\
 u_1, t_1 &= u, t \\
 &= p, t \\
 &= (t, r_2) \text{ Sin } R \\
 &= \text{Tan } B \text{ Sin } B \text{ Sin } R \\
 \therefore \text{Tan } L10 &= \frac{\text{Tan } B \text{ Sin } B \text{ Sin } R}{\text{Sin } B} \\
 &= \text{Tan } B \text{ Sin } R
 \end{aligned}$$

## ANALYTIC PROOFS



## Tangent L3

$$\begin{aligned}
 1. \quad \tan L3 &= \frac{r}{1} \\
 2. \quad &= \frac{l-q}{1} \\
 3. \quad j &= \sin^2 A \\
 4. \quad b_2, c_2 &= \tan A \\
 5. \quad z &= \frac{1}{\cos B} \\
 6. \quad &= \frac{\sin^2 A}{\cos B} \\
 7. \quad l &= \frac{z}{\cos R} \\
 8. \quad &= \frac{\sin^2 A}{\cos B \cos R} \\
 9. \quad q &= (b_2, c_2) \sin R
 \end{aligned}$$

$$\begin{aligned}
 10. \quad &= \tan A \sin R \\
 11. \quad &= \frac{\sin A \sin R}{\cos A} \\
 12. \quad r &= l - q \\
 13. \quad &= \frac{\sin^2 A}{\cos B \cos R} - \frac{\sin A \sin R}{\cos A} \\
 14. \quad (e+z) &= \frac{1}{\cos B} \\
 15. \quad l &= (e+z) \sin R \\
 16. \quad &= \frac{1}{\cos B} \sin R \\
 17. \quad &= \frac{\sin R}{\cos B} \\
 18. \quad \therefore \tan L3 &= \frac{\frac{\sin^2 A}{\cos B \cos R} - \frac{\sin A \sin R}{\cos A}}{\frac{\sin R}{\cos B}}
 \end{aligned}$$

## ANALYTIC PROOFS

$$\begin{aligned}
19. &= \frac{\frac{\sin^2 A \cos A - \sin A \sin R \cos B \cos R}{\cos B \cos R \cos A}}{\frac{\sin R}{\cos B}} \\
20. &= \frac{\sin^2 A \cos A - \sin A \cos^2 R \tan R \cos B}{\cos A \cos^2 R \tan R} \\
21. &= \frac{\sin^2 A \cos A - \sin A \cos^2 R \tan A \cos^2 B}{\cos A \cos^2 R \tan A \cos B} \\
22. &= \frac{\cos A \sin^2 A - \frac{\sin^2 A \cos^2 R \cos^2 B}{\cos A}}{\cos A \cos^2 R \sin A \cos B} \\
23. &= \frac{\frac{\cos^2 A \sin^2 A - \sin^2 A \cos^2 R \cos^2 B}{\cos A}}{\cos A \cos^2 R \sin A \cos B} \\
24. &= \frac{\cos^2 A \sin^2 A - \sin^2 A \cos^2 R \cos^2 B}{\cos A \cos^2 R \sin A \cos B} \\
25. \text{ But, } r_2, b_2 &= \sqrt{\frac{1}{\cos^2 B} + \tan^2 A} \\
26. &= \sqrt{\frac{1}{\cos^2 B} + \frac{\sin^2 A}{\cos^2 A}} \\
27. &= \sqrt{\frac{\cos^2 A + \sin^2 A \cos^2 B}{\cos^2 A \cos^2 B}} \\
28. &= \sqrt{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos A \cos B}} \\
29. \cos R &= \frac{\frac{1}{\cos B}}{\sqrt{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos A \cos B}}} \\
30. &= \frac{\cos A}{\sqrt{\sin^2 A \cos^2 B + \cos^2 A}} \\
&\text{Hence by substitution in No. 24.} \\
31. \tan L_3 &= \frac{\sin^2 A \cos^2 A - \sin^2 A \left( \frac{\cos^2 A}{\sin^2 A \cos^2 B + \cos^2 A} \right) \cos^2 B}{\cos A \left( \frac{\cos^2 A}{\sin^2 A \cos^2 B + \cos^2 A} \right) \sin A \cos B} \\
32. &= \frac{\sin^2 A \cos^2 A (\sin^2 A \cos^2 B + \cos^2 A) - \sin^2 A \cos^2 A \cos^2 B}{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos^2 A \sin A \cos B} \sin^2 A \cos^2 B + \cos^2 A} \\
33. &= \frac{\sin A (\sin^2 A \cos^2 B + \cos^2 A) - \sin A \cos^2 B}{\cos A \cos B} \\
34. &= \frac{\sin A (\sin^2 A \cos^2 B + \cos^2 A - \cos^2 B)}{\cos A \cos B} \\
35. &= \frac{\sin A [\cos^2 B (\sin^2 A - 1) + \cos^2 A]}{\cos A \cos B} \\
36. &= \frac{\sin A [\cos^2 B (-\cos^2 A) + \cos^2 A]}{\cos A \cos B} \\
37. &= \frac{\sin A (\cos^2 A - \cos^2 A \cos^2 B)}{\cos A \cos B} \\
38. &= \frac{\sin A \cos^2 A (1 - \cos^2 B)}{\cos A \cos B} \\
39. &= \frac{\sin A \cos^2 A \sin^2 B}{\cos A \cos B} \\
40. &= \sin A \cos A \sin B \tan B
\end{aligned}$$

## ANALYTIC PROOFS

Tangent  $L_6$ —Refer to Page 22.

1.  $a = \cos A$
2.  $b = \cos^2 A$
3.  $c = \cos A \sin A$
4.  $d = \frac{1}{\sin B}$
5.  $e = \frac{\cos^2 A}{\cos B}$
6.  $f = \sqrt{d^2 + e^2}$
7. 
$$= \frac{\sqrt{\sin^2 B \cos^4 A + \cos^2 B}}{\cos B \sin B}$$
8. Let  $M = \sqrt{\cos^2 B + \cos^4 A \sin^2 B}$  (for convenience)
9. Then  $f = \frac{M}{\cos B \sin B}$
10.  $h = \sqrt{c^2 + f^2}$
11. 
$$= \sqrt{\cos^2 A \sin^2 A + \frac{\sin^2 B \cos^4 A + \cos^2 B}{\cos^2 B \sin^2 B}}$$
12. 
$$= \frac{\sqrt{\cos^2 A \sin^2 A \cos^2 B \sin^2 B + \sin^2 B \cos^4 A + \cos^2 B}}{\cos B \sin B}$$
13. Let  $P = \sqrt{\cos^2 A \sin^2 A \cos^2 B \sin^2 B + \sin^2 B \cos^4 A + \cos^2 B}$
14. Then  $h = \frac{P}{\cos B \sin B}$
15.  $\sin G_4 = \frac{c}{h}$
16. 
$$= \frac{\cos A \sin A \cos B \sin B}{P}$$
17.  $\sin G_2 = \frac{e}{f}$
18. 
$$= \frac{\frac{\cos^2 A}{\cos B}}{\frac{M}{\cos B \sin B}}$$
19. 
$$= \frac{\cos^2 A \sin B}{M}$$
20.  $\cos G_2 = \frac{d}{f}$
21. 
$$= \frac{\frac{1}{\sin B}}{\frac{M}{\cos B \sin B}}$$
22. 
$$= \frac{\cos B}{M}$$
23.  $g = d \cos G_2$

## ANALYTIC PROOFS

$$\begin{aligned}
24. &= \left( \frac{1}{\sin B} \right) \left( \frac{\cos B}{M} \right) \\
25. &= \frac{\cos B}{M \sin B} \\
26. &m = g \sin G_2 \\
27. &= \left( \frac{\cos B}{M \sin B} \right) \left( \frac{\cos A \sin A \cos B \sin B}{P} \right) \\
28. &= \frac{\cos A \sin A \cos^2 B}{M P} \\
29. &k = d \sin G_2 \\
30. &= \left( \frac{1}{\sin B} \right) \left( \frac{\cos^2 A \sin B}{M} \right) \\
31. &= \frac{\cos^2 A}{M} \\
32. &s = \sqrt{k^2 + m^2} \\
33. &= \sqrt{\left( \frac{\cos^2 A}{M} \right)^2 + \left( \frac{\cos A \sin A \cos^2 B}{M P} \right)^2} \\
34. &= \frac{\cos A}{M P} \sqrt{P^2 \cos^2 A + \cos^4 B \sin^2 A} \\
35. &\text{Let } N = \sqrt{P^2 \cos^2 A + \cos^4 B \sin^2 A} \quad (\text{for convenience}) \\
36. &\text{Then } s = \frac{N \cos A}{M P} \\
37. &\sin G_3 = \frac{m}{s} \\
38. &= \frac{\frac{\cos A \sin A \cos^2 B}{M P}}{\frac{N \cos A}{M P}} \\
39. &= \frac{\sin A \cos^2 B}{N} \\
40. &\cos G_3 = \frac{k}{s} \\
41. &= \frac{\frac{\cos^2 A}{M}}{\frac{N \cos A}{M P}} \\
42. &= \frac{P \cos A}{N} \\
43. &n = g \tan (B - G_2) \\
44. &= \left( \frac{\cos B}{M \sin B} \right) \tan (B - G_2) \\
45. &= \frac{\cos B \sin (B - G_2)}{M \sin B \cos (B - G_2)} \\
46. &= \frac{\cos B (\sin B \cos G_2 - \cos B \sin G_2)}{M \sin B (\cos B \cos G_2 + \sin B \sin G_2)}
\end{aligned}$$

## ANALYTIC PROOFS

$$\begin{aligned}
47. &= \frac{\cos B \left( \frac{\sin B \cos B}{M} - \frac{\cos B \cos^2 A \sin B}{M} \right)}{M \sin B \left( \frac{\cos^2 B}{M} + \frac{\cos^2 A \sin^2 B}{M} \right)} \\
48. &= \frac{\cos B (\sin B \cos B - \cos B \cos^2 A \sin B)}{M \sin B (\cos^2 B + \cos^2 A \sin^2 B)} \\
49. &= \frac{\cos B (\cos B - \cos B \cos^2 A)}{M (\cos^2 B + \cos^2 A \sin^2 B)} \\
50. &= \frac{\cos^2 B (1 - \cos^2 A)}{M (\cos^2 B + \cos^2 A \sin^2 B)} \\
51. &= \frac{\cos^2 B \sin^2 A}{M (\cos^2 B + \cos^2 A \sin^2 B)} \\
52. &p = m \tan G_2 \\
53. &t = n - p \\
54. &= n - m \tan G_2 \\
55. &y = t \cos G_2 \\
56. &= (n - m \tan G_2) \cos G_2 \\
57. &v = \frac{m}{\cos G_2} \\
58. &w = t \sin G_2 \\
59. &= (n - m \tan G_2) \sin G_2 \\
60. &x = v + w \\
61. &= \frac{m}{\cos G_2} + (n - m \tan G_2) \sin G_2 \\
&\text{Statement for reduction} \\
62. &\tan L\theta = \frac{y}{x} \\
63. &= \frac{(n - m \tan G_2) (\cos G_2)}{\frac{m}{\cos G_2} + (n - m \tan G_2) \sin G_2} \\
64. &= \frac{(n - m \tan G_2) \cos^2 G_2}{m + (n - m \tan G_2) \sin G_2 \cos G_2} \\
65. &= \frac{(n - m \frac{\sin G_2}{\cos G_2}) \cos^2 G_2}{m + (n - m \frac{\sin G_2}{\cos G_2}) \sin G_2 \cos G_2} \\
66. &= \frac{(n \cos G_2 - m \sin G_2) \cos G_2}{m + (n \cos G_2 - m \sin G_2) \sin G_2} \\
67. &= \frac{n \cos^2 G_2 - m \sin G_2 \cos G_2}{m + n \cos G_2 \sin G_2 - m \sin^2 G_2} \\
68. &= \frac{n \cos^2 G_2 - m \sin G_2 \cos G_2}{m (1 - \sin^2 G_2) + n \cos G_2 \sin G_2} \\
69. &= \frac{n \cos^2 G_2 - m \sin G_2 \cos G_2}{m \cos^2 G_2 + n \cos G_2 \sin G_2}
\end{aligned}$$

## ANALYTIC PROOFS

70.  $\frac{n \cos G_2 - m \sin G_2}{m \cos G_2 + n \sin G_2}$   
Hence by substitution
71.  $\tan L_6 = \frac{\left( \frac{\cos^2 B \sin^2 A}{M(\cos^2 B + \cos^2 A \sin^2 B)} \right) \left( \frac{P \cos A}{N} \right) - \left( \frac{\cos A \sin A \cos^2 B}{M P} \right) \left( \frac{\sin A \cos^2 B}{N} \right)}{\left( \frac{\cos A \sin A \cos^2 B}{M P} \right) \left( \frac{P \cos A}{N} \right) + \left( \frac{\cos^2 B \sin^2 A}{M(\cos^2 B + \cos^2 A \sin^2 B)} \right) \left( \frac{\sin A \cos^2 B}{N} \right)}$
72.  $= \frac{\frac{P \cos^2 B \sin^2 A \cos A}{M P N} - \frac{\cos A \sin^2 A \cos^2 B}{M P N}}{\frac{P \cos^2 B \sin A \cos^2 B}{M P N} + \frac{\cos^2 B \sin^2 A}{M N(\cos^2 B + \cos^2 A \sin^2 B)}}$
73.  $= \frac{P^2 \cos A \cos^2 B \sin^2 A - \cos^4 B \sin^2 A \cos A (\cos^2 B + \cos^2 A \sin^2 B)}{P \cos^2 A \cos^2 B \sin A (\cos^2 B + \cos^2 A \sin^2 B) + P \cos^4 B \sin^2 A}$
74.  $= \frac{\sin^2 A \cos^2 B \cos A [P^2 - \cos^2 B (\cos^2 B + \cos^2 A \sin^2 B)]}{P \sin A \cos^2 B [\cos^2 A (\cos^2 B + \cos^2 A \sin^2 B) + \cos B \sin^2 A]}$
75.  $= \frac{\sin A \cos A [P^2 - \cos^2 B (\cos^2 B + \cos^2 A \sin^2 B)]}{P [\cos^2 A \cos^2 B + \cos^4 A \sin B + \cos^2 B \sin^2 A]}$
76.  $= \frac{\sin A \cos A [P^2 - \cos^2 B (\cos^2 B + \cos^2 A \sin^2 B)]}{P [\cos^2 B (\cos^2 A + \sin^2 A) + \cos^4 A \sin^2 B]}$
77.  $= \frac{\sin A \cos A [P^2 - \cos^2 B (\cos^2 B + \cos^2 A \sin^2 B)]}{P [\cos^2 B + \cos^4 A \sin^2 B]}$
78.  $\cos L_4 = \frac{d}{h}$
79.  $= \frac{\frac{1}{\sin B}}{\frac{\sin B \cos B}{P}}$
80.  $= \frac{\cos B}{P}$
81.  $\therefore P \cos L_4 = \cos B$
82.  $P = \frac{\cos B}{\cos L_4}$
83.  $P^2 = \cos^2 A \sin^2 A \cos^2 B \sin^2 B + \sin^2 B \cos^4 A + \cos^2 B$
84.  $\tan L_6 = \frac{\sin A \cos A \cos L_4 [\cos^2 A \sin^2 A \cos^2 B \sin^2 B + \sin^2 B \cos^4 A + \cos^2 B - \cos^2 B \sin^2 B \cos^2 A]}{\cos B [\cos^2 B + \cos^4 A \sin^2 B]}$
85.  $= \frac{\sin A \cos A \cos L_4 [\sin^2 B \cos^2 B \cos^2 A (\sin^2 A - 1) + \cos^2 B (1 - \cos^2 B) + \sin^2 B \cos^4 A]}{\cos B [\cos^2 B + \cos^4 A \sin^2 B]}$
86.  $= \frac{\sin A \cos A \cos L_4 [-\cos^4 A \sin^2 B \cos^2 B + \cos^2 B \sin^2 B + \sin^2 B \cos^4 A]}{\cos B [\cos^2 B + \cos^4 A \sin^2 B]}$
87.  $= \frac{\sin A \cos A \cos L_4 [\cos^4 A \sin^2 B (1 - \cos^2 B) + \cos^2 B \sin^2 B]}{\cos B (\cos^2 B + \cos^4 A \sin^2 B)}$
88.  $= \frac{\sin A \cos A \cos L_4 (\cos^4 A \sin^4 B + \cos^2 B \sin^2 B)}{\cos B (\cos^2 B + \cos^4 A \sin^2 B)}$
89.  $= \frac{\sin A \cos A \cos L_4 \sin^2 B (\cos^4 A \sin^2 B + \cos^2 B)}{\cos B (\cos^2 B + \cos^4 A \sin^2 B)}$
90.  $= \frac{\sin A \cos A \cos L_4 \sin^2 B}{\cos B}$
91. But,  $\tan L_3 = \sin A \cos A \sin B \tan B$
92.  $= \frac{\sin A \cos A \sin^2 B}{\cos B}$
93.  $\therefore \tan L_6 = \cos L_4 \tan L_3$







## ANALYTIC PROOF OF ANGLE X

## SECOND CASE OF PIPE LINE

$$\frac{1}{2} F = \cos \frac{X}{2} \quad \cos X = 2 \cos^2 \frac{X}{2} - 1$$

$$F = \sqrt{C^2 + E^2}$$

$$C = \sin A_1 + \sin A_2$$

$$E = \sqrt{(\cos A_1 + \cos A_2 \cos B)^2 + (\cos A_2 \sin B)^2}$$

$$\begin{aligned} F &= \sqrt{(\sin A_1 + \sin A_2)^2 + (\cos A_1 + \cos A_2 \cos B)^2 + (\cos A_2 \sin B)^2} \\ &= \sqrt{(\sin^2 A_1 + 2 \sin A_1 \sin A_2 + \sin^2 A_2) + (\cos^2 A_1 + 2 \cos A_1 \cos A_2 \cos B + \cos^2 A_2 \cos^2 B) + (\cos^2 A_2 \sin^2 B)} \\ &= \sqrt{\sin^2 A_1 + \cos^2 A_1 + \cos^2 A_2 (\sin^2 B + \cos^2 B) + \sin^2 A_2 + 2 \cos A_1 \cos A_2 \cos B + 2 \sin A_1 \sin A_2} \\ &= \sqrt{1 + \cos^2 A_2 + \sin^2 A_2 + 2 \cos A_1 \cos A_2 \cos B + 2 \sin A_1 \sin A_2} \\ &= \sqrt{2 + 2 \cos A_1 \cos A_2 \cos B + 2 \sin A_1 \sin A_2} \end{aligned}$$

$$\cos \frac{X}{2} = \frac{1}{2} \sqrt{2 + 2 \cos A_1 \cos A_2 \cos B + 2 \sin A_1 \sin A_2}$$

$$\cos X = \frac{2(2 + 2 \cos A_1 \cos A_2 \cos B + 2 \sin A_1 \sin A_2)}{4} - 1$$

$$= \cos A_1 \cos A_2 \cos B + \sin A_1 \sin A_2$$

When

$A_1$  or  $A_2 = 0$

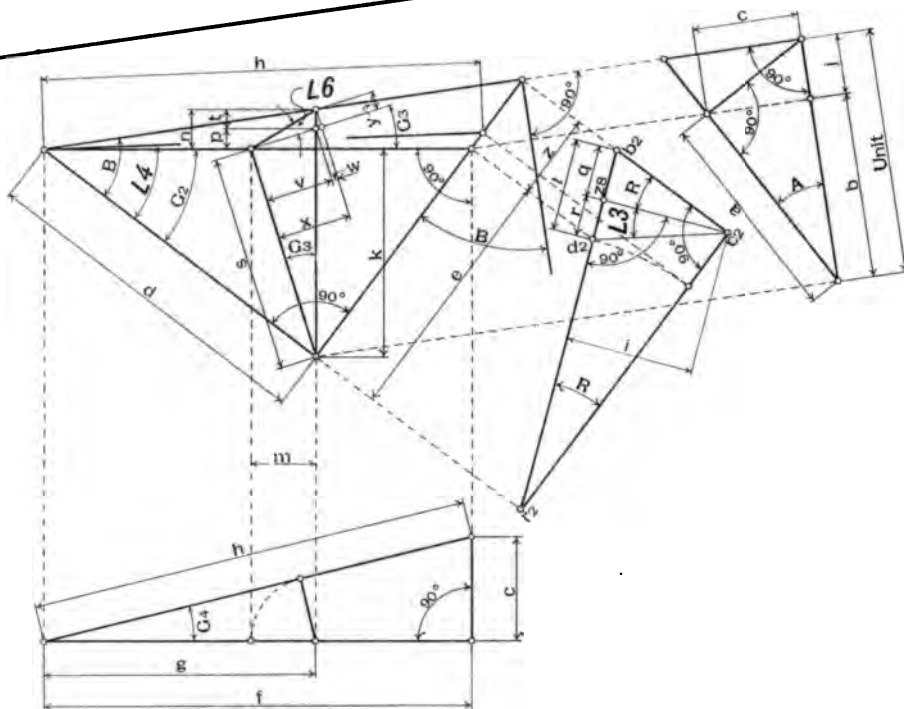
above formula becomes

$\cos X = \cos A \cos B$

which is same as first case



# ANALYTIC PROOFS



## Tangent L3

1.  $\tan L3 = \frac{l}{1}$
2.  $= \frac{l-q}{1}$
3.  $j = \sin^2 A$
4.  $bz, cz = \tan A$
5.  $z = \frac{1}{\cos B}$
6.  $= \frac{\sin^2 A}{\cos B}$
7.  $l = \frac{z}{\cos R}$
8.  $= \frac{\sin^2 A}{\cos B \cos R}$
9.  $q = (bz, cz) \sin R$

10.  $= \frac{\tan A \sin R}{\sin A \sin R}$
11.  $= \frac{\sin A \sin R}{\cos A}$
12.  $r = l - q$
13.  $= \frac{\sin^2 A}{\cos B \cos R} - \frac{\sin A \sin R}{\cos A}$
14.  $(e+z) = \frac{1}{\cos B}$
15.  $l = (e+z) \sin R$
16.  $= \frac{1}{\cos B \sin R}$
17.  $= \frac{\sin R}{\cos B}$
18.  $\therefore \tan L3 = \frac{\frac{\sin^2 A}{\cos B \cos R} - \frac{\sin A \sin R}{\cos A}}{\frac{\sin R}{\cos B}}$

## ANALYTIC PROOFS

$$\begin{aligned}
19. &= \frac{\frac{\sin^2 A \cos A - \sin A \sin R \cos B \cos R}{\cos B \cos R \cos A}}{\frac{\sin R}{\cos B}} \\
20. &= \frac{\sin^2 A \cos A - \sin A \cos^2 R \tan R \cos B}{\cos A \cos^2 R \tan R} \\
21. &= \frac{\sin^2 A \cos A - \sin A \cos^2 R \tan A \cos^2 B}{\cos A \cos^2 R \tan A \cos B} \\
22. &= \frac{\cos A \sin^2 A - \frac{\sin^2 A \cos^2 R \cos^2 B}{\cos A}}{\cos A \cos^2 R \sin A \cos B} \\
23. &= \frac{\frac{\cos^2 A \sin^2 A - \sin^2 A \cos^2 R \cos^2 B}{\cos A}}{\cos A \cos^2 R \sin A \cos B} \\
24. &= \frac{\cos^2 A \sin^2 A - \sin^2 A \cos^2 R \cos^2 B}{\cos A \cos^2 R \sin A \cos B} \\
25. \quad \text{But, } r_2, b_2 &= \sqrt{\frac{1}{\cos^2 B} + \tan^2 A} \\
26. &= \sqrt{\frac{1}{\cos^2 B} + \frac{\sin^2 A}{\cos^2 A}} \\
27. &= \sqrt{\frac{\cos^2 A + \sin^2 A \cos^2 B}{\cos^2 A \cos^2 B}} \\
28. &= \sqrt{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos A \cos B}} \\
29. \quad \cos R &= \frac{1}{\cos B} \\
30. &= \frac{\sqrt{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos A \cos B}}}{\cos A} \\
&\text{Hence by substitution in No. 24.} \\
31. \quad \tan L_3 &= \frac{\sin^2 A \cos^2 A - \sin^2 A \left( \frac{\cos^2 A}{\sin^2 A \cos^2 B + \cos^2 A} \right) \cos^2 B}{\cos A \left( \frac{\cos^2 A}{\sin^2 A \cos^2 B + \cos^2 A} \right) \sin A \cos B} \\
32. &= \frac{\sin^2 A \cos^2 A (\sin^2 A \cos^2 B + \cos^2 A) - \sin^2 A \cos^2 A \cos^2 B}{\frac{\sin^2 A \cos^2 B + \cos^2 A}{\cos^2 A \sin A \cos B} \sin^2 A \cos^2 B + \cos^2 A} \\
33. &= \frac{\sin A (\sin^2 A \cos^2 B + \cos^2 A) - \sin A \cos^2 B}{\cos A \cos B} \\
34. &= \frac{\sin A (\sin^2 A \cos^2 B + \cos^2 A - \cos^2 B)}{\cos A \cos B} \\
35. &= \frac{\sin A [\cos^2 B (\sin^2 A - 1) + \cos^2 A]}{\cos A \cos B} \\
36. &= \frac{\sin A [\cos^2 B (-\cos^2 A) + \cos^2 A]}{\cos A \cos B} \\
37. &= \frac{\sin A (\cos^2 A - \cos^2 A \cos^2 B)}{\cos A \cos B} \\
38. &= \frac{\sin A \cos^2 A (1 - \cos^2 B)}{\cos A \cos B} \\
39. &= \frac{\sin A \cos^2 A \sin^2 B}{\cos A \cos B} \\
40. &= \sin A \cos A \sin B \tan B
\end{aligned}$$







the 1990s, the number of people in the UK who are aged 65 and over has increased by 1.5 million, and the number of people aged 75 and over has increased by 1 million (Office of National Statistics 1999). The number of people aged 65 and over is projected to increase to 6.5 million by 2011, and the number of people aged 75 and over to 3.5 million (Office of National Statistics 1999).

There is a growing awareness of the need to develop services to meet the needs of older people, and a number of initiatives have been developed to address this need. The Department of Health (1999) has published a strategy for older people, which sets out the government's commitment to improve the lives of older people, and to ensure that they are able to live independently and actively for as long as possible.

The strategy identifies a number of key areas for action, including: improving the health and social care services available to older people; promoting independence and active living; and ensuring that older people are able to live in their own homes for as long as possible. The strategy also identifies a number of key challenges, including: the need to develop services that are able to meet the needs of older people who are living with long-term conditions; the need to develop services that are able to meet the needs of older people who are living in care homes; and the need to develop services that are able to meet the needs of older people who are living in the community.

The strategy also identifies a number of key principles, including: the need to ensure that services are able to meet the needs of older people who are living with long-term conditions; the need to ensure that services are able to meet the needs of older people who are living in care homes; and the need to ensure that services are able to meet the needs of older people who are living in the community. The strategy also identifies a number of key objectives, including: to improve the health and social care services available to older people; to promote independence and active living; and to ensure that older people are able to live in their own homes for as long as possible.


The strategy also identifies a number of key actions, including: to improve the health and social care services available to older people; to promote independence and active living; and to ensure that older people are able to live in their own homes for as long as possible. The strategy also identifies a number of key challenges, including: the need to develop services that are able to meet the needs of older people who are living with long-term conditions; the need to develop services that are able to meet the needs of older people who are living in care homes; and the need to develop services that are able to meet the needs of older people who are living in the community.

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A rectangular bookplate with a diagonal line running from the bottom left corner to the middle of the right edge. The text is located in the upper right quadrant, to the right of this diagonal line.

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